

# Generalized Models for Internet Pricing Scheme under Multi Class QoS Networks

*By Fitri maya Puspita*



AENSI Journals

Australian Journal of Basic and Applied Sciences

ISSN:1991-8178

Journal home page: www.ajbasweb.com



## Generalized Models for Internet Pricing Scheme under Multi Class QoS Networks

<sup>1</sup>Irmeilyana, <sup>2</sup>Indrawati, <sup>3</sup>Fitri Maya Puspita, <sup>4</sup>Robinson Sitepu and <sup>5</sup>Rahma Tantia Amelia

<sup>1</sup>Mathematics Department, Faculty of mathematics and Natural Sciences, Sriwijaya University, Jln. Raya Prabumulih KM 32, Inderalaya Ogan Ilir Sumatera Selatan, Indonesia.,

<sup>2</sup>Mathematics Department, Faculty of mathematics and Natural Sciences, Sriwijaya University, Jln. Raya Prabumulih KM 32, Inderalaya Ogan Ilir Sumatera Selatan, Indonesia.

<sup>3</sup>Mathematics Department, Faculty of mathematics and Natural Sciences, Sriwijaya University, Jln. Raya Prabumulih KM 32, Inderalaya Ogan Ilir Sumatera Selatan, Indonesia.

<sup>4</sup>Mathematics Department, Faculty of mathematics and Natural Sciences, Sriwijaya University, Jln. Raya Prabumulih KM 32, Inderalaya Ogan Ilir Sumatera Selatan, Indonesia.

### ARTICLE INFO

#### Article history:

Received 25 June 2014

Received in revised form

8 July 2014

Accepted 25 July 2014

Available online 20 August 2014

#### Keywords:

internet pricing scheme, quality of service, multi class QoS network, base price, quality premium

### ABSTRACT

**Background:** Nowadays, it is a big challenge for Internet Service Provider (ISPs) to deal with the concise pricing scheme under dynamical situations occurring in internet network to maximize the revenue and serve better network services to the customers. The previous research proposed the single link internet pricing scheme for a limited number of users and classes in multi class QoS networks. **Objective:** To generalize the model of internet pricing in multi class QoS network into a number of users and classes **Results:** Compared with previous model, the proposed results show that in model by fixing the base price, varying the quality premium, fixing the user's price sensitivity  $i$  in class  $j$  and varying the price in class  $j$  we obtain the maximum revenue of 4,994.64. **Conclusion:** The Generalized improved models for internet pricing model in multi class QoS network with more users and more classes with the base price and quality premium as a constant or a variable by setting up the user  $i$  sensitivity in class  $j$  ( $\bar{W}_{ij}$ ) and sensitivity in class  $j$  ( $W_j$ ) can be solved to obtain the better maximum profit for according to ISP' preferences. The solutions show the connections between  $\bar{W}_{ij}$  and  $W_j$  as a parameter or variable in maximizing the revenue. In model 1 modified, the highest maximum revenue in case where  $\bar{W}_{ij}$  as parameter and  $W_j$  as variable. Meanwhile, in model 2 modified, the highest revenue is in case where  $\bar{W}_{ij}$  as variable and  $W_j$  as parameter. This is due to the  $Z_{ij}$  values.

© 2014 AENSI Publisher All rights reserved.

**To Cite This Article:** Irmeilyana, Indrawati, F.M. Puspita, R. Sitepu and RT. Amelia. Generalized Models for Internet Pricing Scheme under Multi Class QoS Networks. *Aust. J. Basic & Appl. Sci.*, 8(13): 543-550, 2014

## INTRODUCTION

With the needs to have fast internet, the challenge to provide better quality of internet is essential. The network service quality is determined by the users' satisfactoriness. ISPs have a task to offer better and different QoS to the users to reach the best information quality and also to gain the profit from the available resources. The knowledge to develop the new pricing scheme under user willingness and the providers are provided but only few involve QoS network (Irmeilyana et al., 2014a; Irmeilyana et al., 2014b; Irmeilyana et al., 2014c; Puspita et al., 2011; Puspita et al., 2011; Puspita et al., 2012b; Puspita et al., 2013d).

The latest internet pricing schemes basically comprise three well-known pricing schemes which are flat fee, usage-based, and two-part tariff (Indrawati et al., 2013; Indrawati et al., 2014; Indrawati et al., 2013; Indrawati et al., 2014a; Indrawati et al., 2014b; Wu and Banker, 2010). These three schemes are applied in their discussion under utility function which measures the consumer's satisfactory level. The further optimization of internet pricing schemes are needed in multiservice (Irmeilyana et al., 2013; Irmeilyana et al., 2014a; Puspita et al., 2012a; Puspita et al., 2012c) and multi class QoS networks.

Yang (2004) and Yang et al.(2004; 2004; 2005; 2003) have conducted the research focused on internet pricing on multi class QoS by describing the auction scheme in obtaining the optimal solution. In fact, there exist some parameters affected QoS which can be considered. Based on (Puspita et al., 2013d) by improving and modifying with formulation derived from Yang (2004) and also by considering the utility function

**Corresponding Author:** Irmeilyana, Mathematics Department, Faculty of mathematics and Natural Sciences, Sriwijaya University, Jln. Raya Prabumulih KM 32, Inderalaya Ogan Ilir Sumatera Selatan, Indonesia.  
Ph: +62 813 67784347

originally proposed by Wu and Banker (2010), base price and quality premium as a constant or a variable, index quality, level of QoS and bandwidth needed, we can propose new improved optimal solution.

The studies focused on the improved models for internet pricing scheme in single bottleneck link under multi service network have been proposed (Irmeilyana et al., 2013; Irmeilyana et al., 2014b; Puspita et al. 2012a; Puspita et al. 2012c) and under multi class QoS network (Irmeilyana et al., 2014a; Irmeilyana et al., 2014b; Irmeilyana et al., 2014c; Puspita et al. 2011; Puspita et al. 2011; Puspita et al. 2012b; Puspita et al. 2013a; Puspita et al. 2013d); the improved models in multi bottleneck links (Puspita et al. 2014; Puspita et al. 2013a; Puspita et al. 2013b; Puspita et al. 2013c).. Those studies conducted by setting up the base price and quality premium as a constant or a variable, setting up the QoS level to obtain better maximum profit than previously method described. Those models are applied to two users and classes in multi class QoS networks. In fact, in improving the quality, ISP provides more services and more classes to more users.

This paper basically attempts to offer the generalized optimal solution by applying the improved models for internet pricing in single link with more classes based on Puspita et al. (2014; 2013d) models. The results obtained can assist ISP to choose the best pricing scheme satisfying the users.

**Research Method:**

In this paper, we will solve the optimization problem by using LINGO 11.0. We have parameters and asked to find the variable solutions in maximizing ISP profit. After modeling the formulation, we solve the model by using the tool to get the optimal solution. The solutions are enabling us to interpret and explain the trends in pricing scheme, network, capacity and QoS level.

**Improved Models:**

Models used are adapted from Puspita et al. (2013d) model by distinguishing the model according to the price sensitivity for user *i* in class *j* ( $\tilde{W}_{ij}$ ) and sensitivity in class *j* ( $W_j$ ). We divide into six models namely model 1 original, model 1 modified 1 with  $\alpha$  dan  $\beta$  as a constant, model 1 modified 2 with  $\alpha$  as a constant and  $\beta$  as variable, model 2 original, model 2 modified 1 with  $\alpha$  as variable and  $\beta$  as a constant and model 2 modified 2 with  $\alpha$  dan  $\beta$  as variable

The modified models are divided into three namely

i) If  $\tilde{W}_{ij}$  as parameter and  $W_j$  as variable, then we add the constraint as follows.

$$\tilde{W}_{ij} = k. \tag{1}$$

ii) If  $\tilde{W}_{ij}$  as variable and  $W_j$  as parameter, then we add the constraint as follows.

$$W_j = l. \tag{2}$$

iii) If  $\tilde{W}_{ij}$  as parameter and  $W_j$  as parameter, then add the constraints (1) dan (2).

**RESULTS AND DISCUSSION**

The problem of internet pricing scheme can be solved by using the same model proposed by (Puspita et al., 2013d) with the parameter values are fixed to be  $\alpha_1 = 0.3$ ,  $\alpha_2 = 0.4$  and  $\alpha_3 = 0.5$  when  $\alpha_j$  is as a constant and  $\beta_1=0.01$ ,  $\beta_2=0.05$  and  $\beta_3=0.1$  when  $\beta_j$  is as a constant. The values of  $V_i$  for each model in multi class QoS network are  $V_1=117.09$ ;  $V_2=8,737.61$  and  $V_3=160.71$ . We also set Q value of 30,720 for each class. Other parameters are presented in Table 1.

**Table 1:** Parameter Values in Multi Class QoS Networks.

Parameter	Class (j)		
	1	2	3
$c_j$	4	5	6
$d_j$	0.8	0.9	1
$f$	0.01	0.01	0.01
$g$	0.5	0.5	0.5
$a$	0	0	0
$b$	1	1	1

**Table 2:** Decision Variable Values of Model 1 Original and Model 1 Modified 1.

Variable	Model 1 Original	Model 1 Modifikasi 1		
		$\tilde{W}_{ij}$ Par $W_j$ Var	$\tilde{W}_{ij}$ Var $W_j$ Par	$\tilde{W}_{ij}$ Par $W_j$ Par
$Z_{11}$	0	0	1	1
$Z_{12}$	0	0	1	1
$Z_{13}$	0	0	1	0
$Z_{21}$	1	1	1	1
$Z_{22}$	1	1	1	1
$Z_{23}$	1	1	1	1

$Z_{31}$	1	1	1	1
$Z_{32}$	1	1	1	1
$Z_{33}$	1	1	1	1
$\tilde{W}_{11}$	4	5	4	5
$\tilde{W}_{12}$	4	5	5	5
$\tilde{W}_{13}$	4	5	6	5
$\tilde{W}_{21}$	5	6	4	6
$\tilde{W}_{22}$	5	6	5	6
$\tilde{W}_{23}$	5	6	6	6
$\tilde{W}_{31}$	6	7	4	7
$\tilde{W}_{32}$	6	7	5	7
$\tilde{W}_{33}$	6	7	6	7
$X_1$	10240	10240	10240	10240
$X_2$	10240.17	10240.17	10240	10240

Table 3: Decision Variable Values of Model 1 Original and Model 1 Modified 1(cont'd).

Variabel	Model 1 Original	Model 1 Modifikasi 1		
		$\tilde{W}_{ij}$ Par $W_j$ Var	$\tilde{W}_{ij}$ Var $W_j$ Par	$\tilde{W}_{ij}$ Par $W_j$ Par
2	10240.17	10240.17	10240	10240
$L_{m1}$	0	0	0	0
$L_{m2}$	0	0	0	0
$L_{m3}$	0	0	0	0
$I_1$	-	0.8	0.8	0.8
$I_2$	-	0.9	0.9	0.9
$I_3$	-	1	1	1
$\tilde{X}_{11}$	10240	10240	10240	10240
$\tilde{X}_{12}$	10239.67	10239.67	10240	10240
$\tilde{X}_{13}$	10239.67	10239.67	10240	10239.33
$\tilde{X}_{21}$	10240	10240	10240	10240
$\tilde{X}_{22}$	10240.17	10240.17	10240	10240
$\tilde{X}_{23}$	10240.17	10240.17	10240	10240.33
$\tilde{X}_{31}$	10240	10240	10240	10240
$\tilde{X}_{32}$	10240.17	10240.17	10240	10240
$\tilde{X}_{33}$	10240.17	10240.17	10240	10240.33
$W_1$	5	6	4	4
$W_2$	5	6	5	5
$W_3$	5	6	6	6

Table 2 shows the comparison of variable values of model 1 original and model 1 modified 1 for each case in achieving the optimal solutions. The value of  $Z_{ij}$  represents the user  $i$  in class  $j$ . If  $Z_{ij} = 1$  then the user  $i$  in class  $j$ . On the other hand, if  $Z_{ij} = 0$  then otherwise. According to Table 2 and Table 3 we can see that the decision variable values for each model have quite close values.

Table 4 and 5 explain the comparison of decision variable values of model 1 modified 2 for each case in achieving the optimal solution. We can see that there are same values in each case, and the different value for each case is insignificant. We obtain the highest  $\tilde{X}_{ij}$  and  $X_j$  in model 1 modified 2 for  $\tilde{W}_{ij}$  as parameter and  $W_j$  as variable. The optimal solution for model 1 is presented in Table 6.

Table 4: Variable Decision Values of Model 1 Modified 2.

Variable	Model 1 Modified 2		
	$\tilde{W}_{ij}$ Par $W_j$ Var	$\tilde{W}_{ij}$ Var $W_j$ Par	$\tilde{W}_{ij}$ Par $W_j$ Par
$\beta_1$	0.5	0.5	0.5
$\beta_2$	0.5	0.5	0.5
$\beta_3$	0.5	0.5	0.5
$Z_{11}$	0	1	1
$Z_{12}$	0	1	1
$Z_{13}$	0	1	0
$Z_{21}$	1	1	1
$Z_{22}$	1	1	1
$Z_{23}$	1	1	1
$Z_{31}$	1	1	1
$Z_{32}$	1	1	1
$Z_{33}$	1	1	1
$\tilde{W}_{11}$	5	4	5
$\tilde{W}_{12}$	5	5	5
$\tilde{W}_{13}$	5	6	5

$\tilde{W}_{21}$	6	4	6
$\tilde{W}_{22}$	6	5	6
$\tilde{W}_{23}$	6	6	6
$\tilde{W}_{31}$	7	4	7
$\tilde{W}_{32}$	7	5	7
$\tilde{W}_{33}$	7	6	7
$X_1$	10,240	10,240	10,240
$X_2$	10,240.17	10,240	10,240
$X_3$	10,240.17	10,240	10,240.33
$L_{m1}$	0	0	0
$L_{m2}$	0	0	0

According to the optimal solution presented in Table 6, the maximum profit is achieved in model 1 modified 2 for  $\tilde{W}_{ij}$  as parameter and  $W_j$  as variable of Rp. 3,736.64 (per kbps) through 11 iterations.

Table 5: Variable Decision Values of Model 1 Modified 2(cont'd).

Variable	Model 1 Modified 2		
	$\tilde{W}_{ij}$ Par $W_j$ Var	$\tilde{W}_{ij}$ Var $W_j$ Par	$\tilde{W}_{ij}$ Par $W_j$ Par
$L_{m3}$	0	0	0
$I_1$	0.8	0.8	0.8
$I_2$	0.9	0.9	0.9
$I_3$	1	1	1
$\tilde{X}_{11}$	10,240	10,240	10,240
$\tilde{X}_{12}$	10,239.67	10,240	10,240
$\tilde{X}_{13}$	10,239.67	10,240	10,239.33
$\tilde{X}_{21}$	10,240	10,240	10,240
$\tilde{X}_{22}$	10,240.17	10,240	10,240
$\tilde{X}_{23}$	10,240.17	10,240	10,240.33
$\tilde{X}_{31}$	10,240	10,240	10,240
$\tilde{X}_{32}$	10,240.17	10,240	10,240
$\tilde{X}_{33}$	10,240.17	10,240	10,240.33
$W_1$	6	4	4
$W_2$	6	5	5
$W_3$	6	6	6

Table 6: Model 1 Optimal Solution.

Solver Status	Model 1 Original	Model 1 Modified 1			Model 1 Modified 2		
		$\tilde{W}_{ij}$ Par $W_j$ Var	$\tilde{W}_{ij}$ Var $W_j$ Par	$\tilde{W}_{ij}$ Par $W_j$ Par	$\tilde{W}_{ij}$ Par $W_j$ Var	$\tilde{W}_{ij}$ Var $W_j$ Par	$\tilde{W}_{ij}$ Par $W_j$ Par
Model Class		INLP					
State		Local optimal					
Infeasibility	$3,64 \cdot 10^{-12}$	0	$3,64 \cdot 10^{-12}$	$3,64 \cdot 10^{-12}$	0	0	$3,64 \cdot 10^{-12}$
Iterations	5	5	21	4	11	11	11
		Extended Solver state					
Solver type		Branch & Bound					
Best Objective	3110.89	3733.05	3111.65	3112.05	3736.64	3116.14	3115.64
Objective bound	3110.89	3733.05	3111.65	3112.05	3736.64	3116.14	3115.64
Active	0	0	0	0	0	0	0
Update interval	2	2	2	2	2	2	2
GMU(K)	34	36	34	37	38	36	38
ER(sec)	0	0	0	0	0	0	0

Table 5 presents the comparison of decision variable values of model 2 original and modified 2 for each case in achieving the optimal solutions. In fact, all have very close values. The final bandwidth achieved by user  $i$  in class  $j$  ( $\tilde{X}_{ij}$ ) and bandwidth value for each user in class  $j$  ( $X_j$ ) of model 2 original is the same as model 2 modified 1 with  $\tilde{W}_{ij}$  as parameter and  $W_j$  as variable. If we attempt to compare model 2 modified 1 for  $\tilde{W}_{ij}$  as variable and  $W_j$  as parameter with  $\tilde{W}_{ij}$  as parameter and  $W_j$  as parameter then we have insignificant difference for those models.

Table 7a and 7b explains the decision variable comparison obtained in model 2 modified 2 for each case in obtaining the optimal solution. We can see that some values are the same for each case and some have every close values for each case.

**Table 7a:** The Decision Variable Values of Model 2 *Original* and Model 2 Modified 1.

Variable	Model 2 <i>Original</i>	Model 2 Modified 1		
		$\tilde{W}_{ij}$ Par $W_j$ Var	$\tilde{W}_{ij}$ Var $W_j$ Par	$\tilde{W}_{ij}$ Par $W_j$ Par
$\alpha_1$	1	1	1	1
$\alpha_2$	1	1	1	1
$\alpha_3$	1	1	1	1
$Z_{11}$	0	0	1	1
$Z_{12}$	0	0	1	1
$Z_{13}$	0	0	1	0
$Z_{21}$	1	1	1	1
$Z_{22}$	1	1	1	1
$Z_{23}$	1	1	1	1
$Z_{31}$	1	1	1	1
$Z_{32}$	1	1	1	1
$Z_{33}$	1	1	1	1
$\tilde{W}_{11}$	4	5	4	5
$\tilde{W}_{12}$	4	5	5	5
$\tilde{W}_{13}$	4	5	6	5
$\tilde{W}_{21}$	5	6	4	6
$\tilde{W}_{22}$	5	6	5	6
$\tilde{W}_{23}$	5	6	6	6
$\tilde{W}_{31}$	6	7	4	7
$\tilde{W}_{32}$	6	7	5	7

**Table 7b:** The Decision Variable Values of Model 2 *Original* and Model 2 Modified1(Cont'd).

Variable	Model 2 <i>Original</i>	Model 2 Modified 1		
		$\tilde{W}_{ij}$ Par $W_j$ Var	$\tilde{W}_{ij}$ Var $W_j$ Par	$\tilde{W}_{ij}$ Par $W_j$ Par
$\tilde{W}_{33}$	6	7	6	7
$X_1$	10,240.33	10,240.33	10,240	10,240
$X_2$	10,240.33	10,240.33	10,240	10,240
$X_3$	10,240.33	10,240.33	10,240	10,240.33
$L_{m1}$	0	0	0	0
$L_{m2}$	0	0	0	0
$L_{m3}$	0	0	0	0
$I_1$	0.8	0.8	0.8	0.8
$I_2$	0.9	0.9	0.2	0.9
$I_3$	1	1	1	1
$\tilde{X}_{11}$	10,239.33	10,240.33	10,240	10,240
$\tilde{X}_{12}$	10,239.33	10,240.33	10,240	10,240
$\tilde{X}_{13}$	10,240.33	10,240.33	10,240	10,239.33
$\tilde{X}_{21}$	10,240.33	10,240.33	10,240	10,240
$\tilde{X}_{22}$	10,240.33	10,240.33	10,240	10,240
$\tilde{X}_{23}$	10,240.33	10,240.33	10,240	10,240.33
$\tilde{X}_{31}$	10,240.33	10,240.33	10,240	10,240
$\tilde{X}_{32}$	10,240.33	10,240.33	10,240	10,240
$\tilde{X}_{33}$	10,240.33	10,240.33	10,240	10,240.33
$W_1$	5	6	4	4
$W_2$	5	6	5	5
$W_3$	5	6	6	6

**Table 8a:** Decision Variable Values of Model 2 Modified 2.

Variable	Model 2 Modified2		
	$\tilde{W}_{ij}$ Par $W_j$ Var	$\tilde{W}_{ij}$ Var $W_j$ Par	$\tilde{W}_{ij}$ Par $W_j$ Par
$\alpha_1$	1	1	1
$\alpha_2$	1	1	1
$\alpha_3$	1	1	1
$\beta_1$	0.5	0.5	0.5
$\beta_2$	0.5	0.5	0.5
$\beta_3$	0.5	0.5	0.5
$Z_{11}$	0	1	1
$Z_{12}$	0	1	1
$Z_{13}$	0	1	0
$Z_{21}$	1	1	1
$Z_{22}$	1	1	1
$Z_{23}$	1	1	1
$Z_{31}$	1	1	1
$Z_{32}$	1	1	1

Z <sub>33</sub>	1	1	1
$\bar{W}_{11}$	5	4	5
$\bar{W}_{12}$	5	5	5
$\bar{W}_{13}$	5	6	5
$\bar{W}_{21}$	6	4	6
$\bar{W}_{22}$	6	5	6
$\bar{W}_{23}$	6	6	6

Table 8b: Decision Variable Values of Model 2 Modified 2(cont'd).

Variable	Model 2 Modified2		
	$\bar{W}_{ij}$ Par W <sub>j</sub> Var	$\bar{W}_{ij}$ Var W <sub>j</sub> Par	$\bar{W}_{ij}$ Par W <sub>j</sub> Par
$\bar{W}_{31}$	7	4	7
$\bar{W}_{32}$	7	5	7
$\bar{W}_{33}$	7	6	7
X <sub>1</sub>	10,240.33	10,240	10,240
X <sub>2</sub>	10,240.33	10,240	10,240
2	10,240.33	10,240	10,240.33
L <sub>m,1</sub>	0	0	0
L <sub>m,2</sub>	0	0	0
L <sub>m,3</sub>	0	0	0
I <sub>1</sub>	0.8	0.8	0.8
I <sub>2</sub>	0.9	0.2	0.9
I <sub>3</sub>	1	1	1
$\bar{X}_{11}$	10,240.33	10,240	10,240
$\bar{X}_{12}$	10,240.33	10,240	10,240
$\bar{X}_{13}$	10,240.33	10,240	10,239.33
$\bar{X}_{21}$	10,240.33	10,240	10,240
$\bar{X}_{22}$	10,240.33	10,240	10,240
$\bar{X}_{23}$	10,240.33	10,240	10,240.33
$\bar{X}_{31}$	10,240.33	10,240	10,240
$\bar{X}_{32}$	10,240.33	10,240	10,240
$\bar{X}_{33}$	10,240.33	10,240	10,240.33
W <sub>1</sub>	6	4	4
W <sub>2</sub>	6	5	5
W <sub>3</sub>	6	6	6

Table 9: Optimal Solution of Model 2.

Solver Status	Model 2 Original	Model 2 Modified 1			Model 2 Modified 2		
		$\bar{W}_{ij}$ Par W <sub>j</sub> Var	$\bar{W}_{ij}$ Var W <sub>j</sub> Par	$\bar{W}_{ij}$ Par W <sub>j</sub> Par	$\bar{W}_{ij}$ Par W <sub>j</sub> Var	$\bar{W}_{ij}$ Var W <sub>j</sub> Par	$\bar{W}_{ij}$ Par W <sub>j</sub> Par
Infeasibility	3.64x10 <sup>-12</sup>	3.64x10 <sup>-12</sup>	8.33x10 <sup>-17</sup>	0	3.64x10 <sup>-12</sup>	1.89x10 <sup>-12</sup>	3.64x10 <sup>-12</sup>
Iterations	8	17	7	7	7	6	7
Best Objective	2,078.33	2,493.1	3,118.11	2,702.38	2,495.49	3,121.54	2,705.57
Objective bound	2,078.33	2,493.1	3,118.11	2,702.38	2,495.49	3,121.54	2,705.57
Active	0	0	0	0	0	0	0
Update interval	2	2	2	2	2	2	2
GMU(K)	36	38	36	38	40	38	40
ER(sec)	0	0	0	0	0	0	0

According to optimal solution presented in Table 8, we obtain the maximum profit with  $\bar{W}_{ij}$  as variable and W<sub>j</sub> as parameter in model 2 modified 2 of Rp. 3,121.54 (per kbps) which is solved by 6 iterations as stated in Table 9.

Table 10: Recapitulation of Optimal Solution Model in Multi Class QoS.

Solver Status	Model 1 Modified 2	Model 2 Modified 2
	$\bar{W}_{ij}$ Par W <sub>j</sub> Var	$\bar{W}_{ij}$ Var W <sub>j</sub> Par
Model Class	INLP	
State	Local optimal	
Infeasibility	0	1.89x10 <sup>-12</sup>
Iterations	11	6
Extended Solver Status		
Solver type	Branch & Bound	
Best Objective	3736.64	3121.54
Objective bound	3736.64	3121.54
Active	0	0
Update interval	2	2

$GMU(K)$	38	38
$ER(sec)$	0	0

The results in Table 10 explain the comparison of highest optimal solutions in every model 1 and Model 2 in multi class QoS networks previously described in Table 4 and Table 7a and 7b. The maximum solution is obtained in Model 1 of modification 2 for  $\tilde{W}_{ij}$  as parameter and  $W_j$  as variable with maximum profit of Rp. 3,736.64 (per kbps).

#### Conclusion:

The Generalized improved models for internet pricing model in multi class QoS network with more users and more classes with the base price and quality premium as a constant or a variable by setting up the user  $i$  sensitivity in class  $j$  ( $\tilde{W}_{ij}$ ) and sensitivity in class  $j$  ( $W_j$ ) can be solved to obtain the better maximum profit for according to ISP' preferences. The solutions show the connections between  $\tilde{W}_{ij}$  and  $W_j$  as a parameter or variable in maximizing the revenue. In model 1 modified, the highest maximum revenue in case where  $\tilde{W}_{ij}$  as parameter and  $W_j$  as variable. Meanwhile, in model 2 modified, the highest revenue is in case where  $\tilde{W}_{ij}$  as variable and  $W_j$  as parameter. This is due to the  $Z_{ij}$  values.

#### ACKNOWLEDGEMENT

1

The research leading to this study was financially supported by Directorate of Higher Education Indonesia (DIKTI) for support through Hibah Bersaing Tahun II, 2014.

#### REFERENCES

- Indrawati, Irmeilyana, F.M. Puspita and C.A.Gozali, 2013. Optimasi Model Skema Pembiayaan Internet Berdasarkan Functions of Bandwidth Diminished with Increasing Bandwidth. Paper presented at the Seminar Hasil Penelitian dalam rangka Dies Natalies Universitas Sriwijaya.
- Indrawati, Irmeilyana, F. M. Puspita and C.A. Gozali, 2014. Optimasi Model Skema Pembiayaan Internet Berdasarkan Fungsi Utilitas Perfect Substitute. Paper presented at the Seminar Nasional dan Rapat Tahunan bidang MIPA 2014, Institut Pertanian Bogor, Bogor.
- Indrawati, Irmeilyana, F.M. Puspita and M.P. Lestari, 2013. Optimasi Model Skema Pembiayaan Internet Berdasarkan Fungsi Utilitas Quasi-Linier. Paper presented at the Seminar Hasil Penelitian dalam rangka Dies Natalis Universitas Sriwijaya.
- Indrawati, Irmeilyana, F.M. Puspita and M.P. Lestari, 2014a. Cobb-Douglass Utility Function in Optimizing the Internet Pricing Scheme Model. TELKOMNIKA, 12(1).
- Indrawati, Irmeilyana, F.M. Puspita and M.P. Lestari, 2014b. Perbandingan Fungsi Utilitas Cobb-Douglass Dan Quasi-Linear Dalam Menentukan Solusi Optimal Masalah Pembiayaan Layanan Informasi. Paper presented at the Seminar Nasional Matematika dan Statistika 2014, Universitas Tanjung Pura, Pontianak Kalimantan Barat.
- Irmeilyana, Indrawati, F.M. Puspita and L. Herdayana, 2013. Model yang Diperbaiki dan Solusi Skema Pembiayaan Internet Link Tunggal pada Jaringan Multi Layanan (Multi Service Network). Paper presented at the Seminar Hasil Penelitian Universitas Sriwijaya.
- Irmeilyana, Indrawati, F.M. Puspita and L. Herdayana, 2014a. Improving the Models of Internet Charging in Single Link Multiple Class QoS Networks. Paper presented at the 2014 International Conference on Computer and Communication Engineering (ICOCOE'2014), Melaka, Malaysia.
- Irmeilyana, Indrawati, F.M. Puspita and L. Herdayana, 2014b. The New Improved Models of Single Link Internet Pricing Scheme in Multiple QoS Network. Paper presented at the International Conference Recent trends in Engineering & Technology (ICRET'2014), Batam (Indonesia).
- Irmeilyana, Indrawati, F.M. Puspita and Juniwati, 2014a. Model and optimal solution of single link pricing scheme multiservice network. TELKOMNIKA, 12(1): 173-178.
- Irmeilyana, Indrawati, F.M. Puspita and Juniwati, 2014b. Model and Optimal Solution of Single Link Pricing Scheme Multiservice Network. TELKOMNIKA, 12(1).
- Irmeilyana, Indrawati, F.M. Puspita and Juniwati, 2014c. Model Dan Solusi Optimal Skema Pembiayaan Internet Link Tunggal Pada Jaringan Multi Qos (Multiple Qos Network). Paper presented at the Seminar Nasional dan Rapat Tahunan bidang MIPA 2014, Institut Pertanian Bogor, Bogor.
- Puspita, F. M., K. Seman and B. Sanugi, 2011. Internet Charging Scheme Under Multiple QoS Networks. Paper presented at the The International Conference on Numerical Analysis & Optimization (ICeMATH 2011) 6-8 June 2011, Yogyakarta, Indonesia.
- Puspita, F.M., K. Seman and B.M. Taib, 2011. A Comparison of Optimization of Charging Scheme in Multiple QoS Networks. Paper presented at the 1st AKEPT 1st Annual Young Researchers International



Conference and Exhibition (AYRC X3 2011) Beyond 2020: Today's Young Researcher Tomorrow's Leader 19-20 DECEMBER 2011, PWTC, KUALA LUMPUR.

Puspita, F.M., K. Seman and B.M. Taib, 2014. The Improved Models of Internet Pricing Scheme of Multi Service Multi Link Networks with Various Capacity Links. Paper presented at the 2014 International Conference on Computer and Communication Engineering (ICOCOE'2014), Melaka, Malaysia.

Puspita, F.M., K. Seman, B.M. Taib and Z. Shafii, 2012a. An improved optimization model of internet charging scheme in multi service networks. TELKOMNIKA, 10(3): 592-598.

Puspita, F.M., K. Seman, B.M. Taib and Z. Shafii, 2012b. Models of Internet Charging Scheme under Multiple QoS Networks. Paper presented at the International Conferences on Mathematical Sciences and Computer Engineering 29-30 November 2012, Kuala Lumpur, Malaysia.

Puspita, F.M., K. Seman, B.M. Taib and Z. Shafii, 2012c. A new approach of optimization model on internet charging scheme in multi service networks. International Journal of Science and Technology, 2(6): 391-394.

Puspita, F.M., K. Seman, B.M. Taib and Z. Shafii, 2013a. The Improved Formulation Models of Internet Pricing Scheme of Multiple Bottleneck Link QoS Networks with Various Link Capacity Cases. Paper presented at the Seminar Hasil Penyelidikan Sektor Pengajian Tinggi Kementerian Pendidikan Malaysia ke-3.

Puspita, F.M., K. Seman, B.M. Taib and Z. Shafii, 2013b. An Improved Model of Internet Pricing Scheme of Multi Service Network in Multiple Link QoS Networks. Paper presented at the The 2013 International Conference on Computer Science and Information Technology (CSIT-2013), Universitas Teknologi Yogyakarta.

Puspita, F.M., K. Seman, B.M. Taib and Z. Shafii, 2013c. Improved Models of Internet Charging Scheme of Multi bottleneck Links in Multi QoS Networks. Australian Journal of Basic and Applied Sciences, 7(7): 928-937.

Puspita, F.M., K. Seman, B.M. Taib and Z. Shafii, 2013d. Improved Models of Internet Charging Scheme of Single Bottleneck Link in Multi QoS Networks. Journal of Applied Sciences, 13(4): 572-579.

Wu, S.Y., R.D. Banker, 2010. Best Pricing Strategy for Information Services. Journal of the Association for Information Systems, 11(6): 339-366.

Yang, W., 2004. Pricing Network Resources in Differentiated Service Networks. Phd Thesis. Georgia Institute of Technology.

Yang, W., H. Owen and D.M. Blough, 2004. A Comparison of Auction and Flat Pricing for Differentiated Service Networks. Paper presented at the Proceedings of the IEEE International Conference on Communications.

Yang, W., H.L. Owen and D.M. Blough, 2005. Determining Differentiated Services Network Pricing Through Auctions. Paper presented at the Networking-ICN 2005, 4th International Conference on Networking April 2005 Proceedings, Part I, Reunion Island, France.

Yang, W., H.L. Owen, D.M. Blough and Y. Guan, 2003. An Auction Pricing Strategy for Differentiated Service Network. Paper presented at the Proceedings of the IEEE Global Telecommunications Conference.

# Generalized Models for Internet Pricing Scheme under Multi Class QoS Networks

---

ORIGINALITY REPORT

---

4%

SIMILARITY INDEX

---

PRIMARY SOURCES

---

1	<a href="http://media.neliti.com">media.neliti.com</a> Internet	80 words — 2%
2	<a href="http://documents.irevues.inist.fr">documents.irevues.inist.fr</a> Internet	51 words — 1%
3	<a href="http://seminar.ilkom.unsri.ac.id">seminar.ilkom.unsri.ac.id</a> Internet	12 words — < 1%

---

EXCLUDE QUOTES ON

EXCLUDE MATCHES < 1%

EXCLUDE BIBLIOGRAPHY ON