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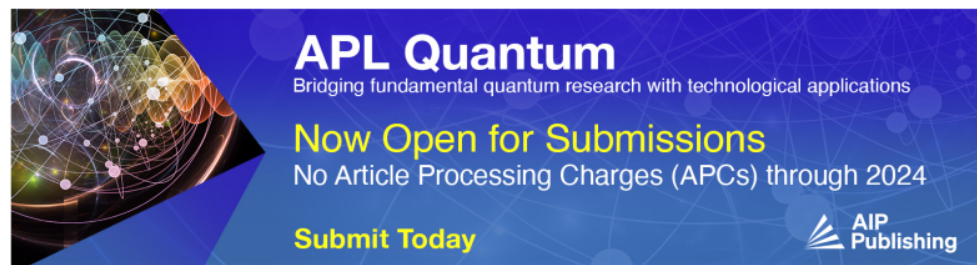
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Optimization of Temporary Disposal Facilities Location with Set Covering Problem Model and Ant Colony Optimization Algorithm in Ilir Barat I District Palembang

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Abstract. The waste problem in Ilir Barat I District arises due to the prominent population of residents who settle. Extensive population results in an increase in the volume of waste produced. Temporary disposal facilities (TDF) are the government's effort to overcome the waste problem. The locations of TDF in Ilir Barat I District are irregular. Therefore this study aims to determine the optimal location of TDF in the Ilir Barat I District by formulating the set covering problem (SCP) model. SCP models developed in this research include the set covering location problem (SCLP) and p-center location problem. We used LINGO programming for the exact approach and the ant colony optimization (ACO) algorithm for the heuristic approach. There are 27 TDF spread across six sub-districts in Ilir Barat I District. From the formulation of the SCP model and the implementation of the ACO algorithm, there are 15 optimal TDF locations in Ilir Barat I District. Based on the results obtained, this study recommends an ACO algorithm for determining the optimal location of TDF because the solution of the ACO algorithm can meet the whole demand point in Ilir Barat I District. The optimal TDF in Ilir Barat I District is TDF Jl. Demang Lebar Daun Titik Sampah Halte in front of Kantor Perdagangan Kota, TDF opposite PS, TDF Jl. Puncak Sekuning, TDF Jl. Bintang beside Bank Mandiri, TDF Jl. Natuna beside BPN, TDF Jl. Angkatan 45 Titik Sampah Simpang Lorong Harisan, TDF Jl. Angkatan 45 Titik Sampah in front of Lorong Persatuan, TDF Jl. Angkatan 45 Titik Sampah opposite Lorong Kejora (Lorong Harapan), TDF Jl. Angkatan 45 in front of Jl. Sang Merah Putih, TDF Simpang Jl. Kaca Piring, TDF Jl. Soekarno Hatta Titik Sampah Simpang Jembatan Kancil Putih, TDF Jl. Demang Lebar Daun Titik Sampah Halte Retensi Brimob, TDF Siguntang, TDF Jl. Srijaya Negara beside Jl. Jaya Sempurna, and TDF Jl. Srijaya Negara Pasar Padang Selasa. All TDF can meet the demand in each sub-district in Ilir Barat I District.

INTRODUCTION

The yearly increase in the number of residents in Palembang city coincides with an increase in the volume of waste produced. Alfian and Phelia [1] revealed that the large population and the diversity of activities in big cities are one of the causes of the emergence of waste problems. Ilir Barat I District has the second highest population in Palembang City. More residents occupying an area will produce more waste [2]. The rate of trash that continues to increase every year is not accompanied by an increase in waste management by the government, so the waste problem still needs to be overcome.

Through the environment and hygiene service (DLHK), Palembang City Government provides TDF to overcome the problem of accumulated waste. The TDF aims to reduce the volume and impact caused by the debris. Improper location of TDF can result in excessive landfilling. Therefore, determining TDF's location is one of the critical indicators in the waste management system. Optimizing location placement is one of the optimization problems [3]. SCP model is an optimization problem to determine the location and number of TDF [4]. SCP is an integer programming model called integer linear programming (ILP), where some or all variables are integers. In everyday life, the SCP model includes: allocating tasks assigned to machines, sharing work with employees, optimizing facility locations to obtain optimal results, and assigning vehicle routes to TDF to maximize distance and cost [5].

We can solve the SCP model using various models, including SCLP and the p-center location problem. SCLP is an optimization model that aims to place the location of a facility along with its number to meet all demand points [6]. Meanwhile, the p-center location problem is an optimization model that aims to determine the location of facilities to minimize the maximum travel distance where each facility must cover all demand points [4]. A p-center location problem is a minimax facility location problem to plan the location of public facilities such as hospitals, fire stations, and other facilities [7].

One of the heuristic methods that can solve SCP [8][9][10][11][12][13][14][15] is ACO. ACO is a heuristic mainly used to solve complex combinatorial optimization problems. The ACO algorithm is adopted from the behavior of ant colonies when searching for food [16]. Ant colonies can find the shortest passage from a food source to their nest using pheromones traces [17]. Pheromones communicate with other ants so that the next ants can follow the route that contains pheromones, and the ants will form the shortest route.

Some previous studies on SCP are in determining the location of public facilities [18][19][20][21][22], including Sitepu *et al.* [6], who optimizes the area of emergency installation locations of hospitals in Palembang City with the SCLP model that recommends five emergency installation locations to meet all demand points. Ayudhya [23] examined the location of humanitarian aid facilities in Nakhon Sri Thammarat and Phatthalung Provinces using the p-Center model. The research result is we need one center of humanitarian assistance in Phra Phrom, two in Mueng Phatthalung and Mueng Nakhon Sri Thammarat, and three h Syukriah *et al.* [24] drafting syrup distribution routes at UD. Bireuen Rice Flower with ACO algorithm. The best route in Bireuen is ant line 7, with a total distance of 105.3 km, while the best route in Lhokseumawe is ant line 10, with a total distance of 122.5 km.

Based on the background, this study discusses optimizing the location of TDF in Ilir Barat I. This study formulated an SCP model including SCLP and p-center location problems that were solved using the LINGO 13.0 application. The SCLP model can minimize the number of TDF to cover all demand points in each sub-district. Then we implemented the ACO algorithm to determine the route and optimal TDF in Ilir Barat I District. Using a broader structure in the ACO algorithm helps find acceptable solutions at this stage of the research process. The solution in this research can become a consideration for DLHK Palembang City in determining the optimal TDF in Ilir Barat I District and a reference for further study in selecting the waste transportation routing.

METHOD

The first step in this study is retrieving distance data between each TDF in Ilir Barat I District from DLHK Palembang City and presented in a data table. Next, we define TDF and sub-district data variables in Ilir Barat I District. We formulate an SCP model consisting of an SCLP model and a p-center location problem model, then find the solution of the model by using the LINGO 13.0 application. For the heuristic approach, we implement the ACO algorithm to determine the optimal location of TDF. The final steps are to analyze the results of the SCP model and ACO algorithm to get the optimal location of TDF in Ilir Barat I District.

RESULT AND DISCUSSION

This section explains the SCLP model, the p-center location problem model, and the implementation of the ACO algorithm.

The Set Covering Location Problem Model

The definition of variables for TDF in Ilir Barat I District annotated with x_j , where $j = 1, 2, 3, \dots, 27$, we can check it in Table 1. Table 1 states that the variable x_j can be worth 0 or 1. Variable value 1 if the TDF exists and is optimal and placed on site j , while it is worth 0 if the TDF exists but is not optimal and is not placed on site j . The definition

of variables for each sub-district in Ilir Barat I District annotated with y_i , where $i = a, b, c, d, e$, we can see it in Table 2.

Regulation of the Minister of Public Works of the Republic of Indonesia Number 03/PRT/M/2013 concerning the Implementation of Waste Infrastructure and Facilities in Handling Household Waste and Similar Waste of Household Waste in Article 32 states that the technical requirements for the distance between TDF are less than or equal to 500 meters. Table 3 shows the distance between TDF in Ilir Barat I District in meters obtained from the DLHK Palembang City.

TABLE 1. Variables definition for TDF in Ilir Barat I District.

| Variable | Name of TDF |
|----------|--|
| x_1 | TDF Jl. PDAM Kelurahan Bukit Lama |
| x_2 | TDF Jl. Sultan Mansyur |
| x_3 | TDF Perumahan Polygon |
| x_4 | TDF Siguntang |
| x_5 | TDF Jl. Demang Lebar Daun Titik Sampah Halte in front of Kantor Perdagangan Kota |
| x_6 | TDF Jl. Srijaya Negara beside Jl. Jaya Sempurna |
| x_7 | TDF Jl. Srijaya Negara Pasar Padang Selasa |
| x_8 | TDF Jl. Natuna beside BPN |
| x_9 | TDF Jl. Bintan beside Bank Mandiri |
| x_{10} | TDF Sampah Liar Simpang 5 DPRD Provinsi in front of RM. Pindang Kuyung |
| x_{11} | TDF Jl. Puncak Sekuning |
| x_{12} | TDF Jl. Aerobik in front of Kantor DPD GOLKAR |
| x_{13} | TDF Simpang Jl. Kaca Piring |
| x_{14} | TDF opposite PS |
| x_{15} | TDF Jl. Kapten A. Rivai Lorong Karya |
| x_{16} | TDF Jl. Angkatan 45 in front of Jl. Sang Merah Putih |
| x_{17} | TDF Jl. Angkatan 45 Titik Sampah in front of Lorong Persatuan |
| x_{18} | TDF Jl. Angkatan 45 Titik Sampah opposite Lorong Kejora (Lorong Harapan) |
| x_{19} | TDF Jl. Angkatan 45 Titik Sampah Simpang Lorong Harisan |
| x_{20} | TDF Jl. Demang Lebar Daun Titik Sampah Halte Retensi Brimob |
| x_{21} | TDF beside Kantor Keuangan |
| x_{22} | TDF Jl. Demang Lebar Daun Titik in front of Kantor Capil |
| x_{23} | TDF Jl. Soekarno Hatta Titik Sampah Simpang Jembatan Kancil Putih |
| x_{24} | TDF Jl. Inspektur Marzuki Titik Sampah Simpang Lorong Pakjo |
| x_{25} | TDF Lapas Anak Pakjo |
| x_{26} | TDF Komplek Rutan Pakjo |
| x_{27} | TDF Jl. Anwar Arsad in front of Indomaret |

TABLE 2. Definition of variables for Sub-District in Ilir Barat I District.

| Variable | Variable Description |
|----------|--------------------------------|
| y_a | Bukit Lama Sub-District |
| y_b | Bukit Baru Sub-District |
| y_c | 26 Ilir D. I Sub-District |
| y_d | Lorok Pakjo Sub-District |
| y_e | Demang Lebar Daun Sub-District |
| y_f | Siring Agung Sub-District |

TABLE 3. Distance between TDF in Ilir Barat I District.

| d_{ij} | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
|----------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| 1 | 0 | 450 | 2600 | 2000 | 3000 | 3400 | 3800 | 3400 | 3600 | 4500 | 4100 | 4200 | 4700 |
| 2 | 450 | 0 | 2300 | 1550 | 2550 | 2950 | 3350 | 3400 | 3600 | 7400 | 4400 | 4990 | 5400 |
| 3 | 2600 | 2300 | 0 | 3800 | 1900 | 2300 | 2700 | 6000 | 6200 | 6750 | 7100 | 7340 | 8640 |
| 4 | 2000 | 1550 | 3800 | 0 | 1000 | 1400 | 1800 | 1800 | 2000 | 2700 | 2300 | 2400 | 1800 |
| 5 | 3000 | 2550 | 1900 | 1000 | 0 | 2400 | 2800 | 3600 | 3800 | 4700 | 4300 | 4400 | 3800 |
| 6 | 3400 | 2950 | 2300 | 1400 | 2400 | 0 | 400 | 2000 | 2200 | 3100 | 2700 | 2800 | 2500 |
| 7 | 3800 | 3350 | 2700 | 1800 | 2800 | 400 | 0 | 3300 | 3500 | 4050 | 4400 | 4640 | 5940 |
| 8 | 3400 | 3400 | 6000 | 1800 | 3600 | 2000 | 3300 | 0 | 200 | 750 | 1100 | 1340 | 2640 |
| 9 | 3600 | 3600 | 6200 | 2000 | 3800 | 2200 | 3500 | 200 | 0 | 550 | 900 | 1140 | 2440 |
| 10 | 4500 | 7400 | 6750 | 2700 | 4700 | 3100 | 4050 | 750 | 550 | 0 | 350 | 590 | 1890 |
| 11 | 4100 | 4400 | 7100 | 2300 | 4300 | 2700 | 4400 | 1100 | 900 | 350 | 0 | 240 | 1540 |
| 12 | 4200 | 4990 | 7340 | 2400 | 4400 | 2800 | 4640 | 1340 | 1140 | 590 | 240 | 0 | 1300 |
| 13 | 4700 | 5400 | 8640 | 1800 | 3800 | 2500 | 5940 | 2640 | 2440 | 1890 | 1540 | 1300 | 0 |
| 14 | 5100 | 5900 | 6800 | 2400 | 4000 | 3100 | 6440 | 3140 | 2940 | 2390 | 2040 | 1800 | 500 |
| 15 | 3100 | 3100 | 5800 | 1300 | 3200 | 1600 | 3100 | 850 | 1100 | 2790 | 2440 | 2200 | 2100 |
| 16 | 4700 | 5400 | 6100 | 1900 | 3300 | 2600 | 6040 | 2740 | 2540 | 1990 | 1640 | 1400 | 1900 |
| 17 | 5900 | 5300 | 5900 | 3100 | 3100 | 3800 | 4700 | 3200 | 4590 | 4040 | 3690 | 3450 | 1700 |
| 18 | 5100 | 5800 | 6500 | 2200 | 3600 | 2900 | 4400 | 2300 | 2300 | 4220 | 1800 | 1900 | 800 |
| 19 | 5600 | 5000 | 5600 | 2800 | 2800 | 3500 | 4400 | 2900 | 2900 | 4340 | 2500 | 2500 | 2450 |
| 20 | 5600 | 5000 | 5600 | 2800 | 2800 | 3500 | 4400 | 2900 | 2800 | 4840 | 2400 | 2500 | 1400 |
| 21 | 4600 | 4000 | 4600 | 3500 | 1800 | 3200 | 3400 | 3600 | 3500 | 5240 | 3100 | 3200 | 2000 |
| 22 | 3900 | 3300 | 3900 | 3600 | 1100 | 2500 | 2700 | 4200 | 4100 | 6240 | 3700 | 3800 | 2700 |
| 23 | 4100 | 3500 | 2700 | 3700 | 1300 | 2700 | 2900 | 5300 | 5200 | 5900 | 5600 | 5700 | 4600 |
| 24 | 6900 | 6100 | 5400 | 5700 | 4000 | 5500 | 5600 | 5800 | 5800 | 7200 | 5000 | 5100 | 3900 |
| 25 | 7100 | 6500 | 6400 | 5300 | 4300 | 5700 | 5900 | 5300 | 5300 | 6500 | 4500 | 4600 | 3500 |
| 26 | 6700 | 6300 | 6300 | 4900 | 3900 | 5300 | 5500 | 5000 | 4900 | 6200 | 4100 | 4200 | 3100 |
| 27 | 5600 | 4900 | 5600 | 4000 | 2700 | 4200 | 4300 | 4100 | 4000 | 5600 | 3600 | 3700 | 2500 |

| d_{ij} | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 |
|----------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| 1 | 5100 | 3100 | 4700 | 5900 | 5100 | 5600 | 5600 | 4600 | 3900 | 4100 | 6900 | 7100 | 6700 | 5600 |
| 2 | 5900 | 3100 | 5400 | 5300 | 5800 | 5000 | 5000 | 4000 | 3300 | 3500 | 6100 | 6500 | 6300 | 4900 |
| 3 | 6800 | 5800 | 6100 | 5900 | 6500 | 5600 | 5600 | 4600 | 3900 | 2700 | 5400 | 6400 | 6300 | 5600 |
| 4 | 2400 | 1300 | 1900 | 3100 | 2200 | 2800 | 2800 | 3500 | 3600 | 3700 | 5700 | 5300 | 4900 | 4000 |
| 5 | 4000 | 3200 | 3300 | 3100 | 3600 | 2800 | 2800 | 1800 | 1100 | 1300 | 4000 | 4300 | 3900 | 2700 |
| 6 | 3100 | 1600 | 2600 | 3800 | 2900 | 3500 | 3500 | 3200 | 2500 | 2700 | 5500 | 5700 | 5300 | 4200 |
| 7 | 6440 | 3100 | 6040 | 4700 | 4400 | 4400 | 4400 | 3400 | 2700 | 2900 | 5600 | 5900 | 5500 | 4300 |
| 8 | 3140 | 850 | 2740 | 3200 | 2300 | 2900 | 2900 | 3600 | 4200 | 5300 | 5800 | 5300 | 5000 | 4100 |
| 9 | 2940 | 1100 | 2540 | 4590 | 2300 | 2900 | 2800 | 3500 | 4100 | 5200 | 5800 | 5300 | 4900 | 4000 |
| 10 | 2390 | 2790 | 1990 | 4040 | 4220 | 4340 | 4840 | 5240 | 6240 | 5900 | 7200 | 6500 | 6200 | 5600 |
| 11 | 2040 | 2440 | 1640 | 3690 | 1800 | 2500 | 2400 | 3100 | 3700 | 5600 | 5000 | 4500 | 4100 | 3600 |
| 12 | 1800 | 2200 | 1400 | 3450 | 1900 | 2500 | 2500 | 3200 | 3800 | 5700 | 5100 | 4600 | 4200 | 3700 |
| 13 | 500 | 2100 | 1900 | 1700 | 800 | 2450 | 1400 | 2000 | 2700 | 4600 | 3900 | 3500 | 3100 | 2500 |
| 14 | 0 | 400 | 1400 | 1650 | 1830 | 1950 | 2450 | 2850 | 3850 | 5750 | 5200 | 5200 | 4400 | 3700 |
| 15 | 400 | 0 | 1000 | 1250 | 1430 | 1550 | 2050 | 2450 | 3450 | 5350 | 7950 | 5600 | 5200 | 4300 |
| 16 | 1400 | 1000 | 0 | 250 | 430 | 550 | 1050 | 1450 | 2450 | 4350 | 3800 | 3400 | 3000 | 2100 |
| 17 | 1650 | 1250 | 250 | 0 | 180 | 300 | 800 | 1200 | 2200 | 4100 | 3700 | 3600 | 2900 | 2300 |
| 18 | 1830 | 1430 | 430 | 180 | 0 | 120 | 620 | 1020 | 2020 | 3920 | 3200 | 2700 | 2700 | 1800 |
| 19 | 1950 | 1550 | 550 | 300 | 120 | 0 | 500 | 900 | 1900 | 3800 | 3100 | 3900 | 3100 | 2000 |
| 20 | 2450 | 2050 | 1050 | 800 | 620 | 500 | 0 | 400 | 1400 | 3300 | 2800 | 2700 | 2300 | 1200 |
| 21 | 2850 | 2450 | 1450 | 1200 | 1020 | 900 | 400 | 0 | 1000 | 2900 | 3100 | 2600 | 2200 | 1100 |
| 22 | 3850 | 3450 | 2450 | 2200 | 2020 | 1900 | 1400 | 1000 | 0 | 1900 | 4500 | 5700 | 3800 | 2600 |
| 23 | 5750 | 5350 | 4350 | 4100 | 3920 | 3800 | 3300 | 2900 | 1900 | 0 | 2600 | 3800 | 3600 | 4800 |
| 24 | 5200 | 7950 | 3800 | 3700 | 3200 | 3100 | 2800 | 3100 | 4500 | 2600 | 0 | 1200 | 850 | 2000 |

| d_{ij} | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 |
|----------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| 25 | 5200 | 5600 | 3400 | 3600 | 2700 | 3900 | 2700 | 2600 | 5700 | 3800 | 1200 | 0 | 400 | 1200 |
| 26 | 4400 | 5200 | 3000 | 2900 | 2700 | 3100 | 2300 | 2200 | 3800 | 3600 | 850 | 400 | 0 | 1300 |
| 27 | 3700 | 4300 | 2100 | 2300 | 1800 | 2000 | 1200 | 1100 | 2600 | 4800 | 2000 | 1200 | 1300 | 0 |

Table 3 shows that the distance between the first and the second TDF is 450 m, between the first and the third TDF is 2,600 m, and so on. The SCLP model is shown in Equation (1) and Constraint (2) to (24).

Minimize Z_{SCLP} that is expressed in Equation (1).

$$Z_{SCLP} = x_1 + x_2 + x_3 + x_4 + x_5 + x_6 + x_7 + x_8 + x_9 + x_{10} + x_{11} + x_{12} + x_{13} + x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} + x_{20} + x_{21} + x_{22} + x_{23} + x_{24} + x_{25} + x_{26} + x_{27} \quad (1)$$

Subject to:

$$x_1 + x_2 \geq 1 \quad (2)$$

$$x_3 \geq 1 \quad (3)$$

$$x_4 \geq 1 \quad (4)$$

$$x_5 \geq 1 \quad (5)$$

$$x_6 + x_7 \geq 1 \quad (6)$$

$$x_8 + x_9 \geq 1 \quad (7)$$

$$x_{10} + x_{11} \geq 1 \quad (8)$$

$$x_{10} + x_{11} + x_{12} \geq 1 \quad (9)$$

$$x_{11} + x_{12} \geq 1 \quad (10)$$

$$x_{13} + x_{14} \geq 1 \quad (11)$$

$$x_{13} + x_{14} + x_{15} \geq 1 \quad (12)$$

$$x_{14} + x_{15} \geq 1 \quad (13)$$

$$x_{16} + x_{17} + x_{18} \geq 1 \quad (14)$$

$$x_{16} + x_{17} + x_{18} + x_{19} \geq 1 \quad (15)$$

$$x_{17} + x_{18} + x_{19} + x_{20} \geq 1 \quad (16)$$

$$x_{19} + x_{20} + x_{21} \geq 1 \quad (17)$$

$$x_{20} + x_{21} \geq 1 \quad (18)$$

$$x_{22} \geq 1 \quad (19)$$

$$x_{23} \geq 1 \quad (20)$$

$$x_{24} \geq 1 \quad (21)$$

$$x_{25} + x_{26} \geq 1 \quad (22)$$

$$x_{27} \geq 1 \quad (23)$$

$$x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8, x_9, x_{10}, x_{11}, x_{12}, x_{13}, x_{14}, x_{15}, x_{16}, x_{17}, x_{18}, x_{19}, x_{20}, x_{21}, x_{22}, x_{23}, x_{24}, x_{25}, x_{26}, x_{27} \in \{0, 1\} \quad (24)$$

Equation (1) is an objective function to minimize the number of candidates for TDF to meet demand points in the Ilir Barat I District. Constraint (2) to (23) ensure that at least one facility is selected to meet each demand point. Constraint (24) is an integer binary constraint. The SCLP model of Ilir Barat I District completed by LINGO 13.0 yielded a value $Z_{SCLP}=15$ with $x_2 = x_3 = x_4 = x_5 = x_7 = x_9 = x_{11} = x_{14} = x_{18} = x_{20} = x_{22} = x_{23} = x_{24} = x_{26} = x_{27} = 1$ as the optimal solution. The location of the optimal TDF candidates results from the SCLP model in Ilir Barat I District, which amounts to 15 TDF, including TDF Jl. Sultan Mansyur, TDF Perumahan Polygon, TDF Siguntang, TDF Jl. Demang Lebar Daun Titik Sampah Halte in front of Kantor Perdagangan Kota, TDF Jl. Srijaya Negara Pasar Padang Selasa, TDF Jl. Bintan beside Bank Mandiri, TDF Jl. Puncak Sekuning, TDF opposite PS, TDF Jl. Angkatan 45 Titik Sampah opposite Lorong Kejora (Lorong Harapan), TDF Jl. Demang Lebar Daun Titik Sampah Halte Retensi Brimob, TDF Jl. Demang Lebar Daun Titik in front of Kantor Capil, TDF Jl. Soekarno Hatta Titik Sampah Simpang Jembatan Kancil Putih, TDF Jl. Inspektur Marzuki Titik Sampah Simpang Lorong Pakjo, TDF Komplek Rutan Pakjo, and TDF Jl. Anwar Arsad in front of Indomaret.

The p-Center Location Problem Model

The p-center location problem model uses optimal TDF location data obtained from the completion of the SCLP model and demand point data in the form of sub-district data in the Ilir Barat I District.

TABLE 4. The optimal TDF from the SCLP model.

| Variable | Name of TDF |
|----------|--|
| x_2 | TDF Jl. Sultan Mansyur |
| x_3 | TDF Perumahan Polygon |
| x_4 | TDF Siguntang |
| x_5 | TDF Jl. Demang Lebar Daun Titik Sampah Halte in front of Kantor Perdagangan Kota |
| x_7 | TDF Jl. Srijaya Negara Pasar Padang Selasa |
| x_9 | TDF Jl. Bintan beside Bank Mandiri |
| x_{11} | TDF Jl. Puncak Sekuning |
| x_{14} | TDF opposite PS |
| x_{18} | TDF Jl. Angkatan 45 Titik Sampah opposite Lorong Kejora (Lorong Harapan) |
| x_{20} | TDF Jl. Demang Lebar Daun Titik Sampah Halte Retensi Brimob |
| x_{22} | TDF Jl. Demang Lebar Daun Titik in front of Kantor Capil |
| x_{23} | TDF Jl. Soekarno Hatta Titik Sampah Simpang Jembatan Kancil Putih |
| x_{24} | TDF Jl. Inspektur Marzuki Titik Sampah Simpang Lorong Pakjo |
| x_{26} | TDF Komplek Rutan Pakjo |
| x_{27} | TDF Jl. Anwar Arsad in front of Indomaret |

Table 4 shows all optimal TDF locations in Ilir Barat I District from the SCLP model, which are notated by x_j , where $j = 2, 3, 5, 7, 9, 11, 14, 18, 20, 22, 23, 24, 26, 27$. It means TDF Jl. Sultan Mansyur, TDF Perumahan Polygon, and so on until TDF Jl. Anwar Arsad in front of Indomaret are optimal TDF. The request point uses sub-district data in Ilir Barat I District, which we can it in Table 2. Meanwhile, we show the distance data from the request point to the optimal TDF location in Table 5.

TABLE 5. The distance between the sub-district and the optimal TDF from the SCLP model.

| d_{jj} | 2 | 3 | 4 | 5 | 7 | 9 | 11 | 14 | 18 | 20 | 22 | 23 | 24 | 26 | 27 |
|----------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| a | 1100 | 1800 | 2400 | 1300 | 2000 | 3600 | 3600 | 4300 | 4200 | 3600 | 2300 | 2600 | 4900 | 4900 | 4000 |
| b | 4400 | 3700 | 3700 | 2400 | 3700 | 5100 | 4900 | 5700 | 4900 | 4300 | 3000 | 1100 | 2800 | 3600 | 3900 |
| c | 2900 | 4400 | 850 | 2500 | 1200 | 700 | 1000 | 1500 | 2500 | 2900 | 2800 | 3400 | 5000 | 4500 | 3500 |
| d | 3300 | 4700 | 1000 | 2400 | 1500 | 950 | 800 | 1200 | 1200 | 1700 | 1800 | 3400 | 3700 | 3200 | 2200 |
| e | 3800 | 3500 | 2800 | 1600 | 2700 | 3400 | 3300 | 3600 | 2600 | 2000 | 750 | 1600 | 2600 | 2900 | 2000 |
| f | 5300 | 4700 | 3900 | 3100 | 4000 | 4300 | 4100 | 4300 | 3300 | 2700 | 2100 | 2200 | 750 | 1600 | 1800 |

Table 5 shows that the distance between sub-district a to the second TDF is 1,100 m, between sub-district a to the third TDF is 1,800 m, and so on. The formulation of the p-center location problem model is Minimize the objective function that is expressed by Equation (25).

$$Z_{p\text{-center}} = L \quad (25)$$

Subject to

$$y_{a,2} + y_{a,3} + y_{a,4} + y_{a,5} + y_{a,7} + y_{a,9} + y_{a,11} + y_{a,14} + y_{a,18} + y_{a,20} + y_{a,22} + y_{a,23} + y_{a,24} + y_{a,26} + y_{a,27} = 1 \quad (26)$$

$$y_{b,2} + y_{b,3} + y_{b,4} + y_{b,5} + y_{b,7} + y_{b,9} + y_{b,11} + y_{b,14} + y_{b,18} + y_{b,20} + y_{b,22} + y_{b,23} + y_{b,24} + y_{b,26} + y_{b,27} = 1 \quad (27)$$

$$y_{c,2} + y_{c,3} + y_{c,4} + y_{c,5} + y_{c,7} + y_{c,9} + y_{c,11} + y_{c,14} + y_{c,18} + y_{c,20} + y_{c,22} + y_{c,23} + y_{c,24} + y_{c,26} + y_{c,27} = 1 \quad (28)$$

$$y_{d,2} + y_{d,3} + y_{d,4} + y_{d,5} + y_{d,7} + y_{d,9} + y_{d,11} + y_{d,14} + y_{d,18} + y_{d,20} + y_{d,22} + y_{d,23} + y_{d,24} + y_{d,26} + y_{d,27} = 1 \quad (29)$$

$$y_{e,2} + y_{e,3} + y_{e,4} + y_{e,5} + y_{e,7} + y_{e,9} + y_{e,11} + y_{e,14} + y_{e,18} + y_{e,20} + y_{e,22} + y_{e,23} + y_{e,24} + y_{e,26} + y_{e,27} = 1 \quad (30)$$

$$y_{f,2} + y_{f,3} + y_{f,4} + y_{f,5} + y_{f,7} + y_{f,9} + y_{f,11} + y_{f,14} + y_{f,18} + y_{f,20} + y_{f,22} + y_{f,23} + y_{f,24} + y_{f,26} + y_{f,27} = 1 \quad (31)$$

$$x_2 + x_3 + x_4 + x_5 + x_7 + x_9 + x_{11} + x_{14} + x_{18} + x_{20} + x_{22} + x_{23} + x_{24} + x_{26} + x_{27} = 15 \quad (32)$$

$$1100y_{a,2} + 1800y_{a,3} + 2400y_{a,4} + 1300y_{a,5} + 2000y_{a,7} + 3600y_{a,9} + 3600y_{a,11} + 4300y_{a,14} + 4200y_{a,18} + 3600y_{a,20} + 2300y_{a,22} + 2600y_{a,23} + 4900y_{a,24} + 4900y_{a,26} + 4000y_{a,27} \leq L \quad (33)$$

$$4400y_{b,2} + 3700y_{b,3} + 3700y_{b,4} + 2400y_{b,5} + 3700y_{b,7} + 5100y_{b,9} + 4900y_{b,11} + 5700y_{b,14} + 4900y_{b,18} + 4300y_{b,20} + 3000y_{b,22} + 1100y_{b,23} + 2800y_{b,24} + 3600y_{b,26} + 3900y_{b,27} \leq L \quad (34)$$

$$2900y_{c,2} + 4400y_{c,3} + 850y_{c,4} + 2500y_{c,5} + 1200y_{c,7} + 700y_{c,9} + 1000y_{c,11} + 1500y_{c,14} + 2500y_{c,18} + 2900y_{c,20} + 2800y_{c,22} + 3400y_{c,23} + 5000y_{c,24} + 4500y_{c,26} + 3500y_{c,27} \leq L \quad (35)$$

$$3300y_{d,2} + 4700y_{d,3} + 1000y_{d,4} + 2400y_{d,5} + 1500y_{d,7} + 950y_{d,9} + 800y_{d,11} + 3600y_{d,14} + 1200y_{d,18} + 1700y_{d,20} + 1800y_{d,22} + 3400y_{d,23} + 3700y_{d,24} + 3200y_{d,26} + 2200y_{d,27} \leq L \quad (36)$$

$$3800y_{e,2} + 3500y_{e,3} + 2800y_{e,4} + 1600y_{e,5} + 2700y_{e,7} + 2400y_{e,9} + 3300y_{e,11} + 3600y_{e,14} + 2600y_{e,18} + 2000y_{e,20} + 750y_{e,22} + 1600y_{e,23} + 2600y_{e,24} + 2900y_{e,26} + 2000y_{e,27} \leq L \quad (37)$$

$$5300y_{f,2} + 4700y_{f,3} + 3900y_{f,4} + 3100y_{f,5} + 4000y_{f,7} + 4300y_{f,9} + 4100y_{f,11} + 4300y_{f,14} + 3300y_{f,18} + 2700y_{f,20} + 2100y_{f,22} + 2200y_{f,23} + 750y_{f,24} + 1600y_{f,26} + 1800y_{f,27} \leq L \quad (38)$$

$$y_{a,2}, y_{b,2}, y_{c,2}, y_{d,2}, y_{e,2}, y_{f,2} \leq x_2 \quad (39)$$

$$y_{a,3}, y_{b,3}, y_{c,3}, y_{d,3}, y_{e,3}, y_{f,3} \leq x_3 \quad (40)$$

$$Y_{a,4}, Y_{b,4}, Y_{c,4}, Y_{d,4}, Y_{e,4}, Y_{f,4} \leq x_4 \quad (41)$$

$$Y_{a,5}, Y_{b,5}, Y_{c,5}, Y_{d,5}, Y_{e,5}, Y_{f,5} \leq x_5 \quad (42)$$

$$Y_{a,7}, Y_{b,7}, Y_{c,7}, Y_{d,7}, Y_{e,7}, Y_{f,7} \leq x_7 \quad (43)$$

$$Y_{a,9}, Y_{b,9}, Y_{c,9}, Y_{d,9}, Y_{e,9}, Y_{f,9} \leq x_9 \quad (44)$$

$$Y_{a,11}, Y_{b,11}, Y_{c,11}, Y_{d,11}, Y_{e,11}, Y_{f,11} \leq x_{11} \quad (45)$$

$$Y_{a,14}, Y_{b,14}, Y_{c,14}, Y_{d,14}, Y_{e,14}, Y_{f,14} \leq x_{14} \quad (46)$$

$$Y_{a,18}, Y_{b,18}, Y_{c,18}, Y_{d,18}, Y_{e,18}, Y_{f,18} \leq x_{18} \quad (47)$$

$$Y_{a,20}, Y_{b,20}, Y_{c,20}, Y_{d,20}, Y_{e,20}, Y_{f,20} \leq x_{20} \quad (48)$$

$$Y_{a,22}, Y_{b,22}, Y_{c,22}, Y_{d,22}, Y_{e,22}, Y_{f,22} \leq x_{22} \quad (49)$$

$$Y_{a,23}, Y_{b,23}, Y_{c,23}, Y_{d,23}, Y_{e,23}, Y_{f,23} \leq x_{23} \quad (50)$$

$$Y_{a,24}, Y_{b,24}, Y_{c,24}, Y_{d,24}, Y_{e,24}, Y_{f,24} \leq x_{24} \quad (51)$$

$$Y_{a,26}, Y_{b,26}, Y_{c,26}, Y_{d,26}, Y_{e,26}, Y_{f,26} \leq x_{26} \quad (52)$$

$$Y_{a,27}, Y_{b,27}, Y_{c,27}, Y_{d,27}, Y_{e,27}, Y_{f,27} \leq x_{27} \quad (53)$$

$$\begin{aligned} & Y_{a,2}, Y_{b,2}, Y_{c,2}, Y_{d,2}, Y_{e,2}, Y_{f,2}, Y_{a,3}, Y_{b,3}, Y_{c,3}, Y_{d,3}, Y_{e,3}, Y_{f,3}, Y_{a,4}, Y_{b,4}, Y_{c,4}, Y_{d,4}, Y_{e,4}, Y_{f,4}, Y_{a,5}, Y_{b,5}, Y_{c,5}, \\ & Y_{d,5}, Y_{e,5}, Y_{f,5}, Y_{a,7}, Y_{b,7}, Y_{c,7}, Y_{d,7}, Y_{e,7}, Y_{f,7}, Y_{a,9}, Y_{b,9}, Y_{c,9}, Y_{d,9}, Y_{e,9}, Y_{f,9}, Y_{a,11}, Y_{b,11}, Y_{c,11}, Y_{d,11}, Y_{e,11}, Y_{f,11}, \\ & Y_{a,14}, Y_{b,14}, Y_{c,14}, Y_{d,14}, Y_{e,14}, Y_{f,14}, Y_{a,18}, Y_{b,18}, Y_{c,18}, Y_{d,18}, Y_{e,18}, Y_{f,18}, Y_{a,20}, Y_{b,20}, Y_{c,20}, Y_{d,20}, Y_{e,20}, Y_{f,20}, Y_{a,22}, \\ & Y_{b,22}, Y_{c,22}, Y_{d,22}, Y_{e,22}, Y_{f,22}, Y_{a,23}, Y_{b,23}, Y_{c,23}, Y_{d,23}, Y_{e,23}, Y_{f,23}, Y_{a,24}, Y_{b,24}, Y_{c,24}, Y_{d,24}, Y_{e,24}, Y_{f,24}, Y_{a,26}, Y_{b,26}, \\ & Y_{c,26}, Y_{d,26}, Y_{e,26}, Y_{f,26}, Y_{a,27}, Y_{b,27}, Y_{c,27}, Y_{d,27}, Y_{e,27}, Y_{f,27} \in \{0,1\} \end{aligned} \quad (54)$$

$$x_2, x_3, x_4, x_5, x_7, x_9, x_{11}, x_{14}, x_{18}, x_{20}, x_{22}, x_{23}, x_{24}, x_{26}, x_{27} \in \{0,1\} \quad (55)$$

$$L \geq 0 \quad (56)$$

Equation (25) is an objective function of minimizing the maximum distance between the request point and the location of the TDF in the Ilir Barat I District. Constraints (26) to (31) stipulate that each request point has only one facility. Constraint (32) displays the number of placements of TDF locations. Constraints (33) to (38) state that the travel distance from the request point to the candidate's location must be less than the maximum travel

distance. Constraints (39) to (53) indicate that the facility may include a demand point. Constraints (54) and (55) state that each variable in the p-center location problem model is binary in value. Constraint (56) states that the maximum travel distance should be non-negative.

The optimal solution of the p-center location problem model is $y_{a,2} = y_{b,23} = y_{c,9} = y_{d,11} = y_{e,22} = y_{f,24} = 1$ which means: 1) The demand in the Bukit Lama Sub-District (y_a) will be placed at TDF Jl. Sultan Mansyur (x_2); 2) The demand in the Bukit Baru Sub-District (y_b) will be placed at TDF Jl. Soekarno Hatta Titik Sampah Simpang Jembatan Kancil Putih (x_{23}); 3) The demand in the 26 Ilir D. I Sub-District (y_c) will be placed at TDF Jl. Bintan beside Bank Mandiri (x_9); 4) The demand in the Lorok Pakjo Sub-District (y_d) will be placed at TDF Jl. Puncak Sekuning (x_{11}); 5) The demand in the Demang Lebar Daun Sub-District (y_e) will be placed at TDF Jl. Demang Lebar Daun Titik in front of Kantor Capil (x_{22}); and 6) The demand in the Siring Agung Sub-District (y_f) will be placed at TDF Jl. Inspektur Marzuki Titik Sampah Simpang Lorong Pakjo (x_{24})

The Implementation of The Ant Colony Optimization Algorithm

The first step of the ACO algorithm is to calculate the visibility value. The data used is the distance data between TDF in Ilir Barat I District, contained in Table 3. The visibility calculation is obtained by Equation (57).

$$\eta_{ij} = \frac{1}{d_{j,j}} \tag{57}$$

Where $\eta_{i,j}$ is the visibility between facility i to facility j and $d_{j,j}$ is the travel distance between facility j .

The visibility value between TDF in Ilir Barat I District can be seen in Table 6.

TABLE 6. Visibility between TDF in Ilir Barat I District.

| η_i | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
|----------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|--------|---------|---------|
| 1 | 0 | 0.00222 | 0.00038 | 0.00050 | 0.00033 | 0.00029 | 0.00026 | 0.00029 | 0.00028 | 0.00022 | 0.0002 | 0.00024 | 0.00021 |
| 2 | 0.00222 | 0 | 0.00043 | 0.00065 | 0.00039 | 0.00034 | 0.00030 | 0.00029 | 0.00028 | 0.00014 | 0.0002 | 0.00020 | 0.00019 |
| 3 | 0.00038 | 0.00043 | 0 | 0.00026 | 0.00053 | 0.00043 | 0.00037 | 0.00017 | 0.00016 | 0.00015 | 0.0001 | 0.00014 | 0.00012 |
| 4 | 0.00050 | 0.00065 | 0.00026 | 0 | 0.00100 | 0.00071 | 0.00056 | 0.00056 | 0.00050 | 0.00037 | 0.0004 | 0.00042 | 0.00056 |
| 5 | 0.00033 | 0.00039 | 0.00053 | 0.00100 | 0 | 0.00042 | 0.00036 | 0.00028 | 0.00026 | 0.00021 | 0.0002 | 0.00023 | 0.00026 |
| 6 | 0.00029 | 0.00034 | 0.00043 | 0.00071 | 0.00042 | 0 | 0.00250 | 0.00050 | 0.00045 | 0.00032 | 0.0003 | 0.00036 | 0.00040 |
| 7 | 0.00026 | 0.00030 | 0.00037 | 0.00056 | 0.00036 | 0.00250 | 0 | 0.00030 | 0.00029 | 0.00025 | 0.0002 | 0.00022 | 0.00017 |
| 8 | 0.00029 | 0.00029 | 0.00017 | 0.00056 | 0.00028 | 0.00050 | 0.00030 | 0 | 0.00500 | 0.00133 | 0.0009 | 0.00075 | 0.00038 |
| 9 | 0.00028 | 0.00028 | 0.00016 | 0.00050 | 0.00026 | 0.00045 | 0.00029 | 0.00500 | 0 | 0.00182 | 0.0011 | 0.00088 | 0.00041 |
| 10 | 0.00022 | 0.00014 | 0.00015 | 0.00037 | 0.00021 | 0.00032 | 0.00025 | 0.00133 | 0.00182 | 0 | 0.0028 | 0.00169 | 0.00053 |
| 11 | 0.00024 | 0.00023 | 0.00014 | 0.00043 | 0.00023 | 0.00037 | 0.00023 | 0.00091 | 0.00111 | 0.00286 | 0 | 0.00417 | 0.00065 |
| 12 | 0.00024 | 0.00020 | 0.00014 | 0.00042 | 0.00023 | 0.00036 | 0.00022 | 0.00075 | 0.00088 | 0.00169 | 0.0041 | 0 | 0.00077 |
| 13 | 0.00021 | 0.00019 | 0.00012 | 0.00056 | 0.00026 | 0.00004 | 0.00017 | 0.00038 | 0.00041 | 0.00053 | 0.0006 | 0.00077 | 0 |
| 14 | 0.00020 | 0.00017 | 0.00015 | 0.00042 | 0.00025 | 0.00032 | 0.00016 | 0.00032 | 0.00034 | 0.00042 | 0.0004 | 0.00056 | 0.00200 |
| 15 | 0.00032 | 0.00032 | 0.00017 | 0.00077 | 0.00031 | 0.00063 | 0.00032 | 0.00118 | 0.00091 | 0.00036 | 0.0004 | 0.00045 | 0.00048 |
| 16 | 0.00021 | 0.00019 | 0.00016 | 0.00053 | 0.00030 | 0.00038 | 0.00017 | 0.00036 | 0.00039 | 0.00050 | 0.0006 | 0.00071 | 0.00053 |
| 17 | 0.00017 | 0.00019 | 0.00017 | 0.00032 | 0.00032 | 0.00026 | 0.00021 | 0.00031 | 0.00022 | 0.00025 | 0.0002 | 0.00029 | 0.00059 |
| 18 | 0.00020 | 0.00017 | 0.00015 | 0.00045 | 0.00028 | 0.00034 | 0.00023 | 0.00043 | 0.00043 | 0.00024 | 0.0005 | 0.00053 | 0.00125 |
| 19 | 0.00018 | 0.00020 | 0.00018 | 0.00036 | 0.00036 | 0.00029 | 0.00023 | 0.00034 | 0.00034 | 0.00023 | 0.0004 | 0.00040 | 0.00041 |
| 20 | 0.00018 | 0.00020 | 0.00018 | 0.00036 | 0.00036 | 0.00029 | 0.00023 | 0.00034 | 0.00036 | 0.00021 | 0.0004 | 0.00040 | 0.00071 |
| 21 | 0.00022 | 0.00025 | 0.00022 | 0.00029 | 0.00056 | 0.00031 | 0.00029 | 0.00028 | 0.00029 | 0.00019 | 0.0003 | 0.00031 | 0.00050 |
| 22 | 0.00026 | 0.00030 | 0.00026 | 0.00028 | 0.00091 | 0.00040 | 0.00037 | 0.00024 | 0.00024 | 0.00016 | 0.0002 | 0.00026 | 0.00037 |
| 23 | 0.00024 | 0.00029 | 0.00037 | 0.00027 | 0.00077 | 0.00037 | 0.00034 | 0.00019 | 0.00019 | 0.00017 | 0.0001 | 0.00018 | 0.00022 |
| 24 | 0.00014 | 0.00016 | 0.00019 | 0.00018 | 0.00025 | 0.00018 | 0.00018 | 0.00017 | 0.00017 | 0.00014 | 0.0002 | 0.00020 | 0.00026 |

| η_i | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
|----------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|--------|---------|---------|
| 25 | 0.00014 | 0.00015 | 0.00016 | 0.00019 | 0.00023 | 0.00018 | 0.00017 | 0.00019 | 0.00019 | 0.00015 | 0.0002 | 0.00022 | 0.00029 |
| 26 | 0.00015 | 0.00016 | 0.00016 | 0.00020 | 0.00026 | 0.00019 | 0.00018 | 0.00020 | 0.00020 | 0.00016 | 0.0002 | 0.00024 | 0.00032 |
| 27 | 0.00018 | 0.00020 | 0.00018 | 0.00025 | 0.00037 | 0.00024 | 0.00023 | 0.00024 | 0.00025 | 0.00018 | 0.0002 | 0.00027 | 0.00040 |

| $\eta_{i,j}$ | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 |
|--------------|---------|---------|---------|--------|---------|---------|----------|--------|---------|---------|----------|---------|---------|--------|
| 1 | 0.00020 | 0.00032 | 0.00021 | 0.0001 | 0.00020 | 0.00018 | 0.00018 | 0.0002 | 0.00026 | 0.00020 | 0.00014 | 0.0001 | 0.00015 | 0.0001 |
| 2 | 0.00017 | 0.00032 | 0.00019 | 0.0001 | 0.00017 | 0.00020 | 0.00020 | 0.0002 | 0.00030 | 0.00020 | 0.00016 | 0.0001 | 0.00016 | 0.0002 |
| 3 | 0.00015 | 0.00017 | 0.00016 | 0.0001 | 0.00015 | 0.00018 | 0.00018 | 0.0002 | 0.00026 | 0.00030 | 0.00019 | 0.0001 | 0.00016 | 0.0001 |
| 4 | 0.00042 | 0.00077 | 0.00053 | 0.0003 | 0.00045 | 0.00036 | 0.00036 | 0.0002 | 0.00028 | 0.00020 | 0.00018 | 0.0001 | 0.00020 | 0.0002 |
| 5 | 0.00025 | 0.00031 | 0.00030 | 0.0003 | 0.00028 | 0.00036 | 0.00036 | 0.0005 | 0.00091 | 0.00070 | 0.00025 | 0.0002 | 0.00026 | 0.0003 |
| 6 | 0.00032 | 0.00063 | 0.00038 | 0.0002 | 0.00034 | 0.00029 | 0.00029 | 0.0003 | 0.00040 | 0.00030 | 0.00018 | 0.0001 | 0.00019 | 0.0002 |
| 7 | 0.00016 | 0.00032 | 0.00017 | 0.0002 | 0.00023 | 0.00023 | 0.00023 | 0.0002 | 0.00037 | 0.00030 | 0.00018 | 0.0001 | 0.00018 | 0.0002 |
| 8 | 0.00032 | 0.00118 | 0.00036 | 0.0003 | 0.00043 | 0.00034 | 0.00034 | 0.0002 | 0.00024 | 0.00010 | 0.00017 | 0.0001 | 0.00020 | 0.0002 |
| 9 | 0.00034 | 0.00091 | 0.00039 | 0.0002 | 0.00043 | 0.00034 | 0.00036 | 0.0002 | 0.00024 | 0.00010 | 0.00017 | 0.0001 | 0.00020 | 0.0002 |
| 10 | 0.00042 | 0.00036 | 0.00050 | 0.0002 | 0.00024 | 0.00023 | 0.00021 | 0.0001 | 0.00016 | 0.00010 | 0.00014 | 0.0001 | 0.00016 | 0.0001 |
| 11 | 0.00049 | 0.00041 | 0.00061 | 0.0002 | 0.00056 | 0.00040 | 0.00042 | 0.0003 | 0.00027 | 0.00010 | 0.00020 | 0.0002 | 0.00024 | 0.0002 |
| 12 | 0.00056 | 0.00045 | 0.00071 | 0.0002 | 0.00053 | 0.00040 | 0.00040 | 0.0003 | 0.00026 | 0.00010 | 0.00020 | 0.0002 | 0.00024 | 0.0002 |
| 13 | 0.00200 | 0.00048 | 0.00053 | 0.0005 | 0.00125 | 0.00041 | 0.00071 | 0.0005 | 0.00037 | 0.00020 | 0.00026 | 0.0002 | 0.00032 | 0.0004 |
| 14 | 0 | 0.00250 | 0.00071 | 0.0006 | 0.00055 | 0.00051 | 0.00041 | 0.0003 | 0.00026 | 0.00010 | 0.00019 | 0.0001 | 0.00023 | 0.0002 |
| 15 | 0.00250 | 0 | 0.00100 | 0.0008 | 0.00070 | 0.00065 | 0.00049 | 0.0004 | 0.00029 | 0.00010 | 0.00013 | 0.0001 | 0.00019 | 0.0002 |
| 16 | 0.00071 | 0.00100 | 0 | 0.0040 | 0.00233 | 0.00182 | 0.00095 | 0.0006 | 0.00041 | 0.00020 | 0.00026 | 0.0002 | 0.00033 | 0.0004 |
| 17 | 0.00061 | 0.00080 | 0.00400 | 0 | 0.00556 | 0.00333 | 0.00125 | 0.0008 | 0.00045 | 0.00020 | 0.00027 | 0.0002 | 0.00034 | 0.0004 |
| 18 | 0.00055 | 0.00070 | 0.00233 | 0.0055 | 0 | 0.00833 | 0.00161 | 0.0009 | 0.00050 | 0.00020 | 0.00031 | 0.0003 | 0.00037 | 0.0005 |
| 19 | 0.00051 | 0.00065 | 0.00182 | 0.0033 | 0.00833 | 0 | 0.00200 | 0.0011 | 0.00053 | 0.00020 | 0.00032 | 0.0002 | 0.00032 | 0.0005 |
| 20 | 0.00041 | 0.00049 | 0.00095 | 0.0012 | 0.00161 | 0.00200 | 0 | 0.0025 | 0.00071 | 0.00030 | 0.00036 | 0.0003 | 0.00043 | 0.0008 |
| 21 | 0.00035 | 0.00041 | 0.00069 | 0.0008 | 0.00098 | 0.00111 | 0.00250 | 0 | 0.00100 | 0.00030 | 0.00032 | 0.0003 | 0.00045 | 0.0009 |
| 22 | 0.00026 | 0.00029 | 0.00041 | 0.0004 | 0.00050 | 0.00053 | 0.00071 | 0.0010 | 0 | 0.00050 | 0.00022 | 0.0001 | 0.00026 | 0.0003 |
| 23 | 0.00017 | 0.00019 | 0.00023 | 0.0002 | 0.00026 | 0.00026 | 0.00030 | 0.0003 | 0.00053 | 0 | 0.00038 | 0.0002 | 0.00028 | 0.0002 |
| 24 | 0.00019 | 0.00013 | 0.00026 | 0.0002 | 0.00031 | 0.00032 | 0.00036 | 0.0003 | 0.00022 | 0.0003 | 0 | 0.0008 | 0.00118 | 0.0005 |
| 25 | 0.00019 | 0.00018 | 0.00029 | 0.0002 | 0.00037 | 0.00026 | 0.00037 | 0.0003 | 0.00018 | 0.00020 | 0.000830 | | 0.00250 | 0.0008 |
| 26 | 0.00023 | 0.00019 | 0.00033 | 0.0003 | 0.00037 | 0.00032 | 0.00043 | 0.0004 | 0.00026 | 0.00020 | 0.00118 | 0.00250 | | 0.0007 |
| 27 | 0.00027 | 0.00023 | 0.00048 | 0.0004 | 0.00056 | 0.00050 | 0.000830 | 0.0009 | 0.00038 | 0.00020 | 0.000500 | 0.0008 | 0.00077 | 0 |

Table 6 shows that the Visibility between the first and the second TDF is 0.00222, between the first and the third TDF is 0.00038, and so on. The next stage is the initialization of parameters which include the Intensity of the ant pheromone trace (τ_{ij}), the ant pheromone control constant (α), the visibility control setting (β), the number of ants (m), the ant pheromone evaporation constant (ρ), and the maximum number of cycles (NC_{\max}). Initialization of parameter values from ACO include $\tau_{ij} = 1, \alpha = 1, \beta = 1, m = 10, \rho = 0.5, NC_{\max} = 1$. Then proceed by generating a random number as the departure point according to the number of ants. The departure point is the starting point of each ant's travel route and is selected by generating a random number [1][25]. After that, it is continued by calculating the probability, which aims to determine the location of the TDF that will then be visited. Probability is calculated by Equation (58).

$$P_{i,j} = \frac{[\tau_{i,j}]^{\alpha} [\eta_{i,j}]^{\beta}}{\sum [\tau_{i,j}]^{\alpha} [\eta_{i,j}]^{\beta}}, j \notin \text{Tabu List} \quad (58)$$

Where $p_{i,j}$ is the probability value of ants visiting facility i to facility j ; $\tau_{i,j}$ is the intensity of ant pheromone trace; $\eta_{i,j}$ is the visibility between facility i to facility j ; α is the ant pheromone control; β is the visibility controller setting; and j is the facility location index.

The cumulative probability value (q_i) is calculated by summing the probability value ($p_{i,j}$) with the previous cumulative probability value (q_{i-1}). After that, it evokes a random number (r_i) at intervals $[0,1]$ as many as the number of ants that have been initialized, and determines the condition of the random number for the selected facility visited next by the rule that is expressed in Equation (59).

$$q_{i-1} \leq r_i \leq q_i \quad (59)$$

Where r_i is the random number of ants i ; q_i is the cumulative probability value of i ; and q_{i-1} is the cumulative probability value of $i-1$.

The process continues by filling in the selected facilities' taboo list so the travel route can be formed. The process of selecting TDF and filling out taboo lists is repeated until the travel route is formed. The next stage is calculating the total distance of the travel route that all ants have traveled based on the taboo list. The data used in Table 3 as data on the distance between TDF in Ilir Barat I District. Ants with the minimum total distance are the optimal solution for this study. The total travel distance of each ant can be seen in Table 7.

Based on Table 7, the minimum travel route was found by ant 5 with a total distance of 58,040 meters. Therefore, the travel route of ants 5 becomes the optimal route of the ACO algorithm. By choosing 15 TDF from the optimal route, the optimal TDF location was obtained due to the ACO algorithm in Ilir Barat I, including TDF Jl. Demang Lebar Daun Titik Sampah Halte in front of Kantor Perdagangan Kota, TDF opposite PS, TDF Jl. Puncak Sekuning, TDF Jl. Bintang beside Bank Mandiri, TDF Jl. Natuna beside BPN, TDF Jl. Angkatan 45 Titik Sampah Simpang Lorong Harisan, TDF Jl. Angkatan 45 Titik Sampah in front of Lorong Persatuan, TDF Jl. Angkatan 45 Titik Sampah opposite Lorong Kejora (Lorong Harapan), TDF Jl. Angkatan 45 in front of Jl. Sang Merah Putih, TDF Simpang Jl. Kaca Piring, TDF Jl. Soekarno Hatta Titik Sampah Simpang Jembatan Kancil Putih, TDF Jl. Demang Lebar Daun Titik Sampah Halte Retensi Brimob, TDF Siguntang, TDF Jl. Srijaya Negara beside Jl. Jaya Sempurna, and TDF Jl. Srijaya Negara Pasar Padang Selasa.

TABLE 7. Total travel distance.

| Ant | Travel Route | Total Distance |
|-----|---|----------------|
| 1 | 18, 20, 11, 8, 9, 16, 17, 19, 4, 6, 23, 5, 2, 1, 25, 27, 26, 24, 10, 12, 13, 7, 22, 3, 15, 14, 21 | 59740 |
| 2 | 22, 20, 21, 14, 27, 15, 8, 9, 18, 17, 2, 1, 13, 11, 12, 10, 7, 4, 6, 25, 5, 23, 24, 16, 19, 26, 3 | 63900 |
| 3 | 18, 19, 5, 24, 23, 26, 8, 16, 15, 14, 11, 12, 10, 9, 13, 21, 20, 17, 1, 4, 7, 6, 25, 27, 3, 2, 22 | 59520 |
| 4 | 10, 9, 8, 15, 5, 18, 19, 17, 2, 4, 21, 11, 1, 25, 27, 20, 6, 7, 24, 26, 14, 16, 3, 13, 23, 22, 12 | 77060 |
| 5 | 5, 14, 11, 9, 8, 19, 17, 18, 16, 13, 23, 20, 4, 6, 7, 15, 2, 1, 21, 26, 25, 27, 24, 22, 12, 10, 3 | 58040 |
| 6 | 10, 4, 6, 7, 20, 16, 17, 13, 26, 23, 11, 12, 2, 1, 27, 9, 8, 19, 18, 24, 22, 5, 3, 15, 21, 25, 14 | 69450 |
| 7 | 3, 6, 12, 26, 24, 27, 18, 19, 10, 9, 8, 23, 5, 7, 15, 14, 20, 13, 21, 17, 16, 25, 1, 2, 22, 4, 11 | 59510 |
| 8 | 12, 11, 10, 14, 7, 4, 20, 13, 27, 17, 21, 18, 25, 26, 22, 2, 1, 9, 19, 15, 5, 23, 6, 16, 3, 8, 24 | 68840 |
| 9 | 26, 24, 3, 10, 7, 22, 15, 8, 20, 27, 21, 18, 12, 11, 6, 1, 2, 17, 19, 13, 4, 5, 14, 9, 16, 25, 23 | 66490 |
| 10 | 24, 3, 2, 15, 25, 21, 1, 17, 20, 19, 16, 18, 12, 14, 13, 22, 9, 5, 6, 26, 27, 11, 8, 10, 23, 7, 4 | 71630 |

There are differences in optimal location between the SCP model results and the implementation of the ACO algorithm. The optimal location by the SCP model is shown in Table 8.

TABLE 8. Location of optimal TDF based on SCP model.

| Sub-District | Location of Optimal TDF |
|-------------------|--|
| Bukit Lama | TDF Jl. Sultan Mansyur |
| | TDF Perumahan Polygon |
| | TDF Siguntang |
| Bukit Baru | TDF Jl. Srijaya Negara Pasar Padang Selasa |
| | TDF Jl. Demang Lebar Daun Titik Sampah Halte in front of Kantor Perdagangan Kota |
| Lorok Pakjo | TDF Jl. Bintang beside Bank Mandiri |
| | TDF Jl. Puncak Sekuning |
| | TDF opposite PS |
| Demang Lebar Daun | TDF Jl. Demang Lebar Daun Titik in front of Kantor Capil |
| | TDF Jl. Angkatan 45 Titik Sampah opposite Lorong Kejora (Lorong Harapan) |
| | TDF Jl. Demang Lebar Daun Titik Sampah Halte Retensi Brimob |
| Siring Agung | TDF Jl. Soekarno Hatta Titik Sampah Simpang Jembatan Kancil Putih |
| | TDF Jl. Inspektur Marzuki Titik Sampah Simpang Lorong Pakjo |
| | TDF Komplek Rutan Pakjo |
| | TDF Jl. Anwar Arsad in front of Indomaret |

Table 8 shows the optimal location of TDF with the SCLP model based on the existing sub-district in Ilir Barat I District. We can see that: 1) Bukit Lama Sub-District consists of 4 optimal TDF; 2) Bukit Baru Sub-District consists of 1 optimal TDF; 3) Lorok Pakjo Sub-District consists of 4 optimal TDF; 4) Demang Lebar Daun Sub-District consists of 2 optimal TDF; 5) Siring Agung Sub-District consists of 4 optimal TDF; and 6) 26 Ilir D.I Sub-District does not have an optimal TDF. We can see the optimal location of the ACO algorithm implementation in Table 9.

TABLE 9. Location of optimal TDF based on the implementation of ACO algorithm.

| Sub-District | Location of Optimal TDF |
|-------------------|--|
| Bukit Lama | TDF Jl. Srijaya Negara beside Jl. Jaya Sempurna |
| | TDF Siguntang |
| | TDF Jl. Srijaya Negara Pasar Padang Selasa |
| Bukit Baru | TDF Jl. Demang Lebar Daun Titik Sampah Halte in front of Kantor Perdagangan Kota |
| | TDF Jl. Natuna beside BPN |
| 26 Ilir D.I | TDF Jl. Bintang beside Bank Mandiri |
| | TDF Jl. Puncak Sekuning |
| | TDF Seberang PS |
| Lorok Pakjo | TDF Jl. Angkatan 45 in front of Jl. Sang Merah Putih |
| | TDF Simpang Jl. Kaca Piring |
| | TDF Jl. Angkatan 45 Titik Sampah opposite Lorong Kejora (Lorong Harapan) |
| Demang Lebar Daun | TDF Jl. Demang Lebar Daun Titik Sampah Halte Retensi Brimob |
| | TDF Jl. Angkatan 45 Titik Sampah Simpang Lorong Harisan |
| | TDF Jl. Angkatan 45 Titik Sampah in front of Lorong Persatuan |
| Siring Agung | TDF Jl. Soekarno Hatta Titik Sampah Simpang Jembatan Kancil Putih |

Table 9 displays the optimal location of TDF with the implementation of the ACO algorithm based on the existing villages in the Ilir Barat I District. We can see that: 1) Bukit Lama Sub-District consists of 3 optimal TDF; 2) Bukit Baru Sub-District consists of 1 optimal TDF; 3) 26 Ilir D.I Sub-District consists of 1 optimal TDF; 4) Lorok Pakjo Sub-District consists of 5 optimal TDF; 5) Demang Lebar Daun Village consists of 4 optimal TDF; and 6) Siring Agung Village consists of 1 optimal TDF.

Based on the SCP model solution, one demand point does not have an optimal TDF, namely 26 Ilir D.I Sub-District. While in the results of the implementation of the ACO algorithm, all demand points have optimal TDF. Therefore, this study recommends a solution from the ACO algorithm because the solution of the ACO algorithm can meet all requests in Ilir Barat I District.

CONCLUSION

The SCP model consisting of SCLP and p-Center Location Problem, as well as the implementation of the ACO algorithm each, produced 15 optimal TDF locations in Ilir Barat I District. However, there are differences in the optimal area between the SCP model results and the implementation of the ACO algorithm. This study recommends the solution from the ACO algorithm because it can meet all requests in Ilir Barat I District, as seen in Table 9. For further research, we recommend implementing other heuristic methods, namely Genetic Algorithms, Greedy Heuristic, Hill Climbing, Simulated Annealing, Particle Swarm Optimization, and Firefly Optimization. In addition, it is necessary to pay attention to other factors, such as the amount of waste transported and the capacity of each TDF.

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