

2	A Comparison of Optimization of Charging Scheme in Multiple QoS Networks
3	Fitri Maya Puspita <sup>1</sup> , and Kamaruzzaman Seman <sup>1*</sup> , Bachok M. Taib <sup>1</sup>
4	<sup>1</sup> Faculty of Science and Technology, Islamic Science University of Malaysia, Nilai, Bandar
5	Baru Nilai, Negeri Sembilan Darul Khusus 71800 Malaysia
6	Email address: pipit140201@yahoo.com.au; <u>drkzaman@usim.edu.my</u> *,
7	bachok@usim.edu.my
8	*corresponding author
9	Abstract. As internet is becoming critical in economics life, Internet Service Providers (ISPs)
10	now deal with high demand to promote good quality information. However, the knowledge to
11	develop new pricing plans that serve both customers and supplier is known, but only a few
12	pricing plans involve QoS networks. This paper will analyze the dynamical situation in
13	network where new proposed pricing plans are offered with QoS networks involved. The plan
14	is attempt to solve multiple QoS Networks scheme as an optimization model by comparing

two models in multiple QoS networks by taking into consideration decision whether the useris admitted to the class or not to obtain profit maximization.

17 Keywords: charging scheme, multiple QoS networks, profit maximization

# 18 **1.0 Introduction**

Recent work on multiple service networks is due to [1]. She described the pricing scheme based auction to allocate QoS and maximize ISP's revenue. According to her, the auction pricing scheme is scalability, efficiency and fairness in sharing resources. The solution of the optimization problem goes from single bottleneck link in the network and then we generalize into multiple bottleneck links using heuristic method. In this paper, she used only single QoS parameter- bandwidth, while in networks, there are many parameters affect QoS that can be considered. Although QoS mechanisms are available in some researches, there are few practical QoS network. Even recently a work in this QoS network [2], it only applies simple network involving one single route from source to destination.

Yang [1] and Yang et al. [3, 4] formulate pricing strategy for differentiated service networks.
In their discussion, they focus on auction algorithm to find the optimal solution. We apply
their mathematical formulation and combine it with mathematical formulation discussed by
Byun and Chatterjee [2].

Basically, we would like to modify the mathematical formulation of [2, 3] since it could also be combined into simpler formulation by taking into consideration the utility function, base price, quality premium, index performance, capacity and also bandwidth required. Next we consider the problem of internet charging scheme as Mixed Binary Integer Nonlinear Programming (MBINLP) to obtain optimal. In this part, we also would like to compare two models in which whether we fix decision variable of user admission to the class or not.

### 39 **2.0 Material and methods**

We attempt to apply optimization techniques in solving the problem in this paper. Like in [5], we also consider the optimization problem as MBINLP that can be solved by using optimization tools. We transform the problem of pricing the internet in multi service networks into optimization model and attempt to solve it to get optimal solution. This solution will help us interpreting the current issues involving pricing, network share, base price, quality premium and also QoS level.

# 46 **3.0 Theory/calculation**

The pricing schemes of the past are mainly responsive pricing that is only charging extra when network congestion indicates that the users have QoS degradation, with size of changes related to degree of congestion by comparing three different schemes for allocating a simple network resource. Firstly use no feedback and user adaptation to the network state. Secondly,
use of a closed-loop form of feedback and adaptation and lastly is a closed loop variation or
tight loop as it shortens the delay in the control loop [5].

53 Other scheme is congestion avoidance algorithm proposed by [6] and also scheme that combines congestion avoidance algorithm and one type of responsive pricing scheme that is 54 smart market mechanism by Network Protocol proposed by [7] and [8]. One important thing 55 why we want to create pricing mechanism is due to reducing congestion. What happens if we 56 cannot avoid congestion? Karp [9] explains problems related to congestion and how to 57 58 control it. If, for instance, there is single flow which is sending packets from source to destination, if it transmits at certain rate, it get dropped packet, but if it chooses to send other 59 rate, it can reach destination. It gets acknowledgment from destination about the received 60 61 packet. But how do we know how much. How can go through? The problem can be 62 formulated as follows. How can the source A, for instance, know and manage its flow over continuing certain time, meaning that time is divided into duration length of time like 63 64 explained in [10] and [11].

Others dealing with analysis of pricing strategy are to optimize profits, do not raise profits by 65 guiding us to efficient pricing strategy which can control the congestion. Tuffin [12], Ros & 66 Tuffin [13] and Odlyzko [14] also proposed Paris metro pricing scheme for charging the 67 68 network. In this case, the different service class will have different price. The user has choice 69 to choose channels to travel and price to pay. The scheme basically makes use of user to partition into classes and move to other class it found same service from other class with 70 lower unit price. But still, they only consider with the case of single network which is not 71 72 suitable with current internet. Meanwhile, Altmann & Chu [15] offer new pricing plan that gives benefit to ISP and users. This plan is combination of flat rate and usage based pricing. 73 In this plan, user will get benefit from unlimited access by choosing higher QoS and at the 74

rs same time ISP is able to reduce its peak load. The drawback is still due to lack of information how that plans can be adopted into multiple route networks. For the next generation internet, the availability of fast transportation of data is required. The multicast communication can decrease due to limitation of bandwidth. So we need QoS specification and compute optimal routes to a multi-constrained problem, by using greedy algorithm such as meta-heuristics algorithm, like suggested in [16].

### 81 **4.0 Results and Discussions**

The idea basically generates from [1, 2, 3, 4] for single QoS network and also we also use utility function adopted by [1, 3, 4] (see in [17]).

84 **4.1** Assumptions

Assume that there is only one single network from source to destination since concentrate on service pricing scheme. Assume that the routing schemes are already set up by the ISP. As [1] pointed out, we have 2 parts of utility function namely, base cost which does not depend on resource consumption and cost which depends on resource consumption. The utility function has characteristics as marginal profit as function of bandwidth decreasing with increasing bandwidth. The Objective of ISP is to obtain maximized revenue subject to constraints based on system' available resources.

### 92 **4.2 Mathematical Formulation**

93 We have parameters as follows:

- 94  $\alpha_j$  : base price for class *j* can set up as fixed price or varies.
- 95  $\beta_j$  : quality premium of class j that has  $I_j$  service performance
- 96 Q : total bandwidth
- 97  $V_i$  : minimum bandwidth required by user *i*
- 98
- 99

100	Decision variables are as follows:						
101	$Z_{ij} = \begin{cases} 1, \text{ if user } i \text{ is admitted to class } j \\ 0, & \text{otherwise} \end{cases}$						
102	$X_{ij}$	$X_{ij}$ : Final bandwidth obtained by user <i>i</i> for class <i>j</i>					
103	$L_{m_j}$	$L_{m_j}$ : Minimum bandwidth for class <i>j</i>					
104	$W_{j}$	: Price sensitivity for class $j$					
105	$I_j$	: Quality index of class <i>j</i>					
106	$X_j$ : Bandwidth assigned to each individual user in class <i>j</i>						
107	$W_{ij}$	Price sensitivity for user $i$ in class $j$					
108							
109	The fir	rst mathematical model will be					
110		$Max P_{ij}.U_{ij} = \sum_{j} \sum_{i} (\alpha_j + \beta_j . I_j) w_j \log \frac{x_{ij}}{L_{m_j}}.Z_{ij}$	(4.1)				
111	Subjec	ct to					
112		$(\sum_{j}\sum_{i}X_{ij}) \le Q$	(4.2)				
113		$X_{ij} \ge L_{m_j} - (1 - Z_{ij})$	(4.3)				
114		$W_j \le W_{ij} + (1 - Z_{ij})$	(4.4)				
115		$X_{ij} \geq V_i - (1 - Z_{ij})$	(4.5)				
116		$X_{ij} \geq X_j - (1 - Z_{ij})$	(4.6)				
117		$X_{ij} \ge Z_{ij}$	(4.7)				
118		$X_{ij} \ge 0$	(4.8)				
119		$L_{m_j} \ge 0$	(4.9)				
120		$W_j \ge 0$	(4.10)				
121		$X_{ij} \leq X_j$	(4.11)				
122		$Z_{ij} = \begin{cases} 1, if user \ i \ is \ admitted \ to \ class \ j \\ 0, otherwise \end{cases}$	(4.12)				

123 
$$\alpha_j \ge \alpha_{j-1}, j > 1 \tag{4.13}$$

$$125 \qquad \qquad 0 \le W_{ij} \le c \tag{4.15}$$

126 
$$\alpha_j + \beta_j . I_j \ge \alpha_{j-1} + \beta_{j-1} . I_{j-1}, j > 1$$
 (4.16)

$$127 0 \le I_j \le d (4.17)$$

Where *a* and *b* are predetermined value of lower bound and upper bound base price respectively, *c* is predetermined value of upper bound price sensitivity for user *i* at class *j* respectively. Also, the value of *d* is as the upper bound of quality index.

131 We also have the second mathematical model that is

132 
$$Max P_{ij} U_{ij} = \sum_{j} \sum_{i} (\alpha_j Z_{ij} + \beta_j I_j) w_j \log \frac{X_{ij}}{L_{m_j}}$$
(4.18)

133 subject to (4.2)-(4.12) and (4.15).

134 Objective function (4.1) and (4.18) basically states that ISP wants to maximize its revenue from total sum of price and its utility function with  $\alpha_i$  varies and  $\alpha_i$  to be fixed respectively. 135 Constraint (4.2) tells us that total final bandwidth of all users cannot exceed the total 136 bandwidth available. Constraint (4.3) states that bandwidth obtained by user *i* should exceed 137 minimum bandwidth for class j if user i is admitted to class j or otherwise. Constraint (4.4) 138 139 tells us about price sensitivity for class *j* should be less than the price sensitivity for user *i* in 140 class j if user i is admitted to class j. Constraint (4.5) gives the information about bandwidth 141 obtained by client *i* for class *j* should exceed minimum bandwidth required by user *i* if user *i* is admitted to class *j*. Constraint (4.6) tells us that bandwidth obtained by user *i* in class *j*. 142 should exceed bandwidth assigned to each individual user in class *j* if user *i* is admitted to 143 class j. Constraint (4.7) shows that bandwidth obtained by user i in class j should be greater 144 145 than the availability of user i in class j and should be nonnegative (4.8). Nonnegativity requirement occurs in price sensitivity (4.10) and minimum bandwidth for class *j* in (4.9). 146 Constraint (4.11) shows that bandwidth obtained by user i in class j should not exceed 147

bandwidth assigned to each individual user in class j. Constraint (4.12) tells us the value of 148 whether the user *i* is admitted to class *j* or not. Constraint (4.13) shows that base price for *j* 149 class is more than base price for j-1 class with j>1. Constraint (4.14) tells us the range of base 150 price (a and b) is lower bound and upper bound of predetermined base price, respectively. 151 Constraint (4.15) states the price sensitivity of user i in class j lies between range of 0 and 152 predetermined value (c) of price sensitivity for user i. Constraint (4.16) shows that the 153 summation of price and quality premium to yield perfect service for *j* class should exceed the 154 one in (j - 1) class with j > 1. Constraint (4.17) shows that the range of index quality should lie 155 156 between 0 and 1 with predetermined d value set up by ISP.

## 157 **4.3 Solutions in Multiple Classes**

We begin with introducing two classes and two users, so j = 2 and i = 2. We set up following conditions as shown in Table 1. Table 2 describes the parameter quantities that are used in both models. We also show the numerical result of both models for each case in Table 3.

In Model 1 and Model 2, as Table 3 shown, only one user is admitted to either class 1 or class
2. Basically it means that for 2 classes, only one user can utilize the class. That user can
choose which class that more benefit for him.

In Model 1, case 1 and case 4 with  $W_{11}>W_{21}$  and  $W_{12}>W_{22}$  we slightly obtain higher value than in case 2 and case 3. It means that by setting up lower price sensitivity for user *i* in previous class, ISP will gain more profit.

167 Next, in Model 2, objective value of 250.92 is achieved for all cases. But in case 3 and case 4, 168 there exist the very small infeasibilities showing the amount that shows the constraint 169 violation. To have best solution ISP can either to choose case 1 or case 2 for their preferences 170 with 0 infeasibilities.

171 If we compare between 2 models, it is obvious that Model 2 will utilize maximum revenue 172 for ISP by fixing  $\alpha$  and  $\beta$  values. In ISP point of view, this condition is achieved when ISP would like to recover the cost and user is still able to select the class that fulfils theirpreferences and budgets.

175 On the other side, Model 1 obtains lower revenue than Model 2. Again, if ISP chooses to 176 apply model 1, ISP will be able to compete in the market, when there is market competition 177 by taking  $\alpha$  value to be varies and user can select the class that fits with their budget and 178 preference by taking  $\beta$  value to be fixed.

#### 179 **5.0 Conclusions**

The model represented shows the connection between bandwidth required, bandwidth obtained and QoS by giving the assumptions and data; we can find the optimal solution with profit maximization. ISP has choices to whether adopt Model 1 or Model 2 according their priorities. However, due to assumptions, we have limited the model into static optimal solution and cannot be dynamic solution where we should have various demands for capacity (peak and off-peak).

### 186 Acknowledgment

This research was partially supported by FRGS scheme grant promoted by MOHE, Malaysia.
The authors would also like to thank to the editor and referees for their valuable comments
and suggestion.

# 190 **References**

191 [1] Yang W. Pricing network resources in differentiated service networks. Ph.D. thesis.
192 School of Electrical and Computer Engineering. Georgia Institute of Technology; 2004.

[2] Byun J, Chatterjee S. A strategic pricing for quality of service (QoS) network business.
Proceedings of the Tenth Americas Conference on Information Systems New York; 2004.

[3] Yang W, Owen H, Blough DM, Guan Y. An auction pricing strategy for differentiated
service network. Proceedings of the IEEE Global Telecommunications Conference; 2003.

197 [4] Yang W, Owen H, Blough DM. A comparison of auction and flat pricing for
198 differentiated service networks. Proceedings of the IEEE International Conference on
199 Communications; 2004.

[5] Mackie-Mason JK, Murphy L, Murphy J. The role of responsive pricing in the internet. In
Bailey J and McKnight L, editors. Internet Economics, Cambridge MIT Press; 1996: p.
202 279-304.

[6] Jacobson V. Congestion avoidance and control. Proc. ACM SIG-COMM.88 Symp,
Stanford, CA; 1988.

[7] Kelly FP, Maulloo AK, Tan DKH. Rate control for communication networks: shadow
 prices, proportional fairness and stability. Journal of Operations Research Society
 1998;49:302-237.

[8] Henderson T, Crowcroft J, Bhatti S. Congestion pricing paying your way in
communication networks. IEEE Internet Computing 2001;5:96-85.

[9] Karp R. Graph Theory, Combinatorics and algorithms interdisciplinary applications. In
Golumbic, M. C. & Hartman, I. B.-A, editors. Optimization problems related to internet
congestion control. New York, Springer Science; 2005, p.1-16.

[10] Fulp EW, Reeves DS. The economic impact of network pricing intervals. Proceedings
of the Workshop Advanced Internet Charging and QoS Technology (ICQT). Zurich,
Switzerland; 2002.

- [11] Yuksel M, Kalyanaraman S, Sikdar B. Effect of pricing intervals on the congestionsensitivity network service prices. Troy, New York, Rensselaer Polytechnic Institute
  Troy, New York ECSE Nets Lab. Tech. Rep. ECSE-NET-2002-1; 2002.
- [12] Tuffin B. Charging the internet without bandwidth reservation: an overview and
  bibliography of mathematical approaches. Journal of Information Science and
  Engineering 2003;19:903-786.
- [13] Ros D, Tuffin B. A mathematical model of the paris metro pricing scheme for charging
   packet networks. Computer Networks: The International Journal of Computer and
   Telecommunications Networking Special issue: Internet economics: Pricing and policies
   2004;46:146-73.
- [14] Odlyzko A. Paris metro pricing for the internet. Proceedings of 1<sup>st</sup> ACM Conference on
   Electronic Commerce; 1998.
- [15] Altmann J, Chu K. How to charge for network service-flat-rate or usage-based? Special
  Issue on Networks and Economics, Computer Networks Journal 2001;36:734-519.
- [16] Ali NB, Molnár M, Belghith A. multi-constrained qos multicast routing optimization.
  Rennes Cedex, Institut De Recherche En Informatique Et Systèmes Aléatoires; 2008.
- [17] Puspita FM, Seman, K, Sanugi, B. Internet charging scheme under multiple qos
   networks. Proceeding of The International Conference on Numerical Analysis and
   Optimization (ICeMATH2011). Yogyakarta, Indonesia; 2011.

TABLE 1. Conditions of the Model 1 and Model 2

Case 1	Case 2	Case 3	Case 4
$V_1 > V_2$	$V_1 < V_2$	$V_1 > V_2$	$V_1 < V_2$
$0 \le W_{11} \le 8$	$0 \leq W_{11} \leq 7$	$0 \le W_{11} \le 7$	$0 \leq W_{11} \leq 8$
$0 \leq W_{12} \leq 8$	$0 \leq W_{12} \leq 7$	$0 \leq W_{12} \leq 7$	$0 \leq W_{12} \leq 8$
$0 \le W_{21} \le 7$	$0 \leq W_{21} \leq 8$	$0 \le W_{21} \le 8$	$0 \le W_{21} \le 7$
$0 \le W_{22} \le 7$	$0 \leq W_{22} \leq 8$	$0 \leq W_{22} \leq 8$	$0 \leq W_{22} \leq 7$

**TABLE 2.** Parameter Quantities

	Model 1				Model 2			
	Case 1	Case 2	Case 3	Case 4	Case 1	Case 2	Case 3	Case 4
Q	100							
$V_1$	6	5	6	5	6	5	6	5
$V_2$	5	6	5	6	5	6	5	6
$\beta_1$	0.01							
$\beta_2$	0.02							
$\alpha_1$	-	-	-	-	0.2			
$\alpha_2$	-	-	-	-	0.3			

TABLE 3. Computation Results for each case of Two Models

	Model		Model	
	1		2	
	original	modified	original	modified
GMU(K)	29	30	29	29
ER(sec)	0	0	0	0
Obj val(\$)	126.13	126.12	250.92	250.92
Iter	7	20	30	22
$\alpha_1(\$)$	0.3	0.3	fixed	
<i>α</i> <sub>2</sub> (\$)	0.3	0.3	fixed	
$I_1$	0.9	0.9	0.9	0.9
$I_2$	0.8	0.8	0.8	0.8
$W_1$	8	8	8	8
$W_2(bps)$	8	8	8	8
<i>X</i> <sub>11</sub> (bps)	25.5	24.5	25	25
<i>X</i> <sub>21</sub> (bps)	24.5	25.5	25	25
<i>X</i> <sub>12</sub> (bps)	25.5	24.5	25	25
<i>X</i> <sub>22</sub> (bps)	24.5	25.5	25	25
$L_{m1}(bps)$	0.01	0.01	0.01	0.01
$L_{m2}(bps)$	0.01	0.01	0.01	0.01
$Z_{11}$	1	0	1	0
$Z_{12}$	1	0	1	0
Z <sub>21</sub>	0	1	0	1
Z <sub>22</sub>	0	1	0	1
$W_{11}$	8	8	8	8
$W_{12}$	7	7	7	7
$W_{21}$	8	8	8	8
$W_{22}$	7	7	7	7
Infeasibilities	0	0	0	