

# Improving the Models of Internet Charging in Single Link Multiple Class QoS Networks

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## Abstract

In this paper, an improved internet charging scheme in multiple QoS networks will be discussed. The objective is to obtain better solution than previous results conducted by previous research. ISPs need a new charging scheme to maximize the revenue and provide better services to customers. The model is set up by fixing the fixed base price, varying the quality premium and fixing the sensitivity price for user in each class. The model is considered as Mixed Integer Nonlinear Programming (MINLP) and that can be solved by LINGO 11.0 to obtain the optimal solutions. We compare three cases of original, modified one and modified two models depending with the fixing or varying parameters or variables. The results show that by improving the pricing scheme model, the user's sensitivity price in modified two cases will yield maximum profit for ISPs.

## 82.1. Introduction

Previous works on pricing scheme of QoS networks is due to [1–4]. They described the pricing scheme based auction to allocate QoS and maximize ISP's revenue. The solution of the optimization problem goes from single bottleneck link in the network and then they generalized into multiple bottleneck links using heuristic method. In their study, they used single QoS parameter-bandwidth. In their discussion, they focus on auction algorithm to find the optimal solution. Based on their idea, it is attempted to improve their mathematical formulation and combine it with mathematical formulation discussed by Byun and Chatterjee [5] (see in [6–11]) to show that by improving the models, ISP improve the profit, with the advantages of availability of base price, quality premium and quality premium to be measured.

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Recent studies have also been conducted to address problem of multiple service network, other kind of pricing scheme in network. Sain and Herpers [12] discussed problem of pricing in multiple service networks. They solve the internet pricing by transforming the model into optimization model and solved using Cplex software. Also, [13–15] discussed the new approach and new improved model of and got better results in getting profit maximization of ISP.

Although QoS mechanisms are available in some researches, there are few practical QoS network. Even recently a work in this QoS network proposed by [1–4], it only applies simple network involving one single route from source to destination.

So, the contribution is created by improving the mathematical formulation of to be simpler formulation in single link by taking into consideration the utility function, base price as fixed price or variable, quality premium as fixed prices and variable, index performance, capacity in one link, bandwidth required and also the user price sensitivity. The problem of internet charging scheme is considered as Mixed Integer Nonlinear Programming (MINLP) to obtain optimal solution by using LINGO 11.0 software. In this part, the comparison of two models is conducted in which whether decision variable is to be fixed of user admission to the class or not. This study focuses to fix the user's price sensitivity in each class. We consider cases of base price to be fixed and the quality premium to be fixed or vary depends on what target ISP would achieve. The Objective of ISP is to obtain maximum profit.

## 82.2. Research Method

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The idea basically generates from [1–5] and are improved in single link multi class QoS networks. We attempt to improve the models when we consider the cases to fix the user price sensitivity in each class.

The steps are taken as follows.

1. Determine the parameters and decision variables for original and modified models.
2. Determine the constraints for the models.
3. Determine the model formulation of Steps 1 and 2.
4. Form the model formulation of base price and quality premium as the constant value and base price as the constant and quality premium as the variable.
5. Analyze the results and conclude the results.

## 82.3. Results and Discussion

### 82.3.1. Assumptions

Assume that there is only one single network from source to destination since concentrate on service pricing scheme. Assume that the routing schemes are already set up by the ISP. As [2] pointed out, we have 2 parts of utility function namely, base cost which does not depend on resource consumption and cost which depends on resource consumption. The parameters and decision variables we set up are presented in Tables 82.1 and 82.2.

**Table 82.1**

Parameters for each case of internet charging scheme

Parameter for original model	
$Q$	Total bandwidth
$V_i$	Minimum bandwidth needed by user $i$
$\alpha_j$	Base price for class $j$
Parameter for model modified 1 ( $\alpha, \beta$ constants)	
$\alpha_j$	Base price for class $j$
$\beta_j$	Premium quality having service performance $f_j$
$Q$	Total bandwidth
$V_i$	Minimum bandwidth needed by user $i$
$c_j$	Upper bound value for user $i$ sensitivity price in class $j$
$d_j$	Upper bound for quality index in class $j$
Parameter for model modified 2 ( $\alpha$ constant, $\beta$ variable)	
$Q$	Total bandwidth
$V_i$	Minimum bandwidth needed by user $i$
$\alpha_j$	Base price for class $j$
$c_j$	Upper bound value for user $i$ sensitivity price in class $j$
$d_j$	Upper bound value for quality index in class $j$
$f_i$	Lower bound for premium quality in class $j$
$g_i$	Upper bound for premium quality in class $j$

**Table 82.2**

Decision variables for each case of internet charging scheme

Variable for original model	$L_{Mj}$ : Minimum bandwidth for class $j$
	$W_j$ : Sensitivity price for class $j$
	$X_j$ : Final bandwidth for class $j$
Variable for modified model with $\alpha$ and $\beta$ parameters	$L_{Mj}$ : Minimum bandwidth for class $j$
	$W_j$ : Sensitivity price for class $j$
	$X_j$ : Final bandwidth for class $j$
	$I_j$ : Quality index of class $j$
Variable for modified model with $\alpha$ parameter and $\beta$ variable	$L_{Mj}$ : Minimum bandwidth for class $j$
	$W_j$ : Sensitivity price for class $j$
	$X_j$ : Final bandwidth for class $j$
	$I_j$ : Quality index of class $j$
	$\beta_j$ : Premium quality of class $j$ having service performance of $I_j$

**82.3.2. Model Formulation**

The model formulation follows from [10] except for and  $W_j$  we modify by varying or fixing the prices, for each case of original, modified and modified 1 with additional constraints if we set up and  $W_j$  as the parameters as follows.

82.1  
82.2

**82.3.3. The Solution for Original Model**

In Table 82.3, the values of decision variables are given for original model. Final bandwidth ( $X_j$ ) of user  $i$  is 1.234568. Minimum bandwidth for and is 1.234568 kbps. Sensitivity prices for class 1 and class 2, respectively ( $W_1$  dan  $W_2$ ) are 1.234568. We varies the base price 0.2/kbps and 0.3/kbps for all cases to promote the ISP goal to compete in market. Table 82.4 presents the solver status of the solver. Best objective is reached on value of 1.

**Table 82.3**

Decision variable values for original model proposed by [2]

Decision variables values

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**Decision variables values**

$\alpha_1$	0.2		1.234568
$\alpha_2$	0.3		1.234568
$\beta_1$	–		1.234568
$\beta_2$	–		1.234568
$Z_{11}$	1		1.234568
$Z_{12}$	1		1.234568
$Z_{21}$	1	$X_1$	1.234568
$Z_{22}$	1	$X_2$	1.234568
	1.234568	$I_1$	–
	1.234568	$I_2$	–
	1.234568	$W_1$	1.234568
	1.234568	$W_2$	1.234568

**Table 82.4**

Solver status of original model proposed by [2].

Solver status	Model class	INLP
	State	Local optimal
	Infeasibility	0
	Iterations	4
Extended solver state	Solver type	Branch and bound
	Active	0
	Update interval	2
	GMU (K)	28
	ER (sec)	1
	Best objective	1
	Objective bound	1
	ESS	0
	TSI	4

Generated Memory Used (GMU) in Table 82.4 shows that the number of allocated memory used to run the solver. For original model, we have GMU of 28 K. Elapsed Runtime (ER) explains that the total time needed to solve the models and is affected by other application running in the system. ER is 1 s in 4 iterations. We got total profit of only 1 unit price.

**82.3.4. The Solutions for Modified Model with  $\alpha$  and  $\beta$  Fixed**

We modified the models into 3 groups when  $W_j$  and as parameters,  $W_j$  as and as variable and lastly when  $W_j$  as variable with as parameter. Table 82.5 explains the variable values for modified models. We obtain final bandwidth () for each user is 400.346 kbps. Premium quality for user 1 is 0.01 and for user 2 of 0.02. Minimum bandwidth and is 0.01 kbps. The price sensitivity for class 1 and 2 respectively ( $W_1$  and  $W_2$ ) are 13 when  $W_j$  as variable and as parameter. We obtain  $W_1 = 10$  and  $W_2 = 12$  when  $W_j$  and  $W_{ij}$  as parameters also  $W_j$  as variable and  $W_{ij}$  as parameter. It means that ISP can vary the base price of 0.2 unit price/kbps and 0.3 unit price/kbps, for all cases to compete in the market.

Table 82.5

Decision variable values for modified model with  $\alpha$  and  $\beta$  fixed

Variable	Modified model with $\alpha$ and $\beta$ fixed		
	$W_j$ Par Par	$W_j$ Par Var	$W_j$ Var Par
$\alpha_1$	0.2	0.2	0.2
$\alpha_2$	0.3	0.3	0.3
$\beta_1$	0.01	0.01	0.01
$\beta_2$	0.02	0.02	0.02
$Z_{11}$	1	1	0
$Z_{12}$	1	1	0
$Z_{21}$	1	1	1
$Z_{22}$	1	1	1
$W_1$	10	10	13
$W_2$	12	12	13
	12	10	12
	12	12	12
	15	10	15
	15	12	15
	400.346	400.346	400.346
	400.346	400.346	400.346
	400.346	400.346	400.346
	400.346	400.346	400.346
	0.01	0.01	0.01
	0.01	0.01	0.01
$X_1$	400.346	400.346	400.346
$X_2$	400.346	400.346	400.346
$I_1$	0.9	0.9	0.9
$I_2$	0.8	0.8	0.8

The highest GMU in this model is 29 K for each case as stated in Table 82.6. ER is 1 s when  $W_j$  and  $W_{ij}$  as parameter. Also, ER = 0 s for  $W_j$  as variable and as parameter, and last case when  $W_j$  as variable and  $W_{ij}$  as parameter. ESS is 0 since the solver applies the branch and bound solver. We can see that ISP can gain the maximum profit of 551.62 unit price if ISP sets  $W_j$  as variable and as parameter to enable ISP to recover cost.

Table 82.6

Solver status for modified model with  $\alpha$  and  $\beta$  fixed

Solver status	$W_j$ Par and Par	$W_j$ Par Var	$W_j$ Var Par
Model class	INLP		

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Solver status	$W_j$ Par and Par	$W_j$ Par Var	$W_j$ Var Par
State	Local optimal		
Infeasibility	7.38964e-012	7.38964e-012	0
Iterations	5	5	7
Solver type	Branch and bound		
Active	0	0	0
Update interval	2	2	2
GMU (K)	29	29	29
ER (sec)	1	0	0
Best objective	467.34	467.34	551.62
Objective bound	467.34	467.34	551.62
ESS	0	0	0
TSI	5	5	7

### 82.3.5. The Solutions for Modified Model with $\alpha$ Fixed and $\beta$ Vary

When we set up the modified model with  $\alpha$  fixed and  $\beta$  vary, we group it into three categories namely when  $W_j$  and as parameter,  $W_j$  as parameter and as variable, dan lastly when  $W_j$  as variable and as variable. Table 82.7 shows the result of decision variables when we set up the modified model with  $\alpha$  fixed and  $\beta$  vary. Final bandwidth () obtained by the users is 400.346 kbps. Premium quality for user 1 is 0.04 and for user 2 is 0.03. Minimum bandwidth for and is 0.01 kbps. Price sensitivity for class 1 and 2 ( $W_1$  dan  $W_2$ ) respectively is 13 when  $W_j$  as variable and as parameter while  $W_1 = 10$  dan  $W_2 = 12$  when  $W_j$  and  $W_{ij}$  as parameter and also when  $W_j$  as variable and  $W_{ij}$  as parameter. ISP enables to vary the base into 0.2/kbps dan 0.3/kbps to promote the available classes.

**Table 82.7**

Decision variables for modified model with  $\alpha$  fixed and  $\beta$  vary

Var	Modified Model with $\alpha$ Fixed and $\beta$ Vary		
	$W_j$ Par Par	$W_j$ Par Var	$W_j$ Var Par
$\alpha_1$	0.2	0.2	0.2
$\alpha_2$	0.3	0.3	0.3
$\beta_1$	0.04	0.04	0.04
$\beta_2$	0.03	0.03	0.03
$Z_{11}$	1	1	0
$Z_{12}$	1	1	0
$Z_{21}$	1	1	1
$Z_{22}$	1	1	1
$W_1$	10	10	13
$W_2$	12	12	13
	12	10	12
	12	12	12
	10	15	

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Modified Model with  $\alpha$  Fixed and  $\beta$  Vary

Var	$W_j$ Par	$W_j$ Var	$W_j$ Par	$W_j$ Var
15	400.346	400.346	12	15
	400.346	400.346		
	400.346	400.346		
	400.346	400.346		
	400.346	400.346		
0.01	400.346	400.346	0.01	0.01
	400.346	400.346		
	400.346	400.346		
	400.346	400.346		
$X_1$	400.346	400.346	400.346	400.346
$X_2$	400.346	400.346	400.346	400.346
$I_1$	0.9	0.9	0.9	0.9
$I_2$	0.8	0.8	0.8	0.8

The highest GMU presented in Table 82.8 is 30 K when  $W_j$  as parameter and  $W_j$  as variable, meanwhile GMU = 29 K when  $W_j$  and as parameter, also when  $W_j$  as variable and  $W_j$  as parameter. ER is 0 s for the case when  $W_j$  and  $W_j$  as parameter, while ER = 1 s for  $W_j$  as variable and as parameter, also  $W_j$  as variable and  $W_j$  as parameter. ESS is 0 for all cases. ISP can obtain maximum profit of 551.69 unit price when ISP sets up the case when  $W_j$  as variable and as parameter to enable ISP to recover cost.

Table 82.8

Solver status of modified model with  $\alpha$  fixed and  $\beta$  vary

Solver status	$W_j$ Par	$W_j$ Par	$W_j$ Var
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Model Class	NLP		
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State	Local optimal		
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Infeasibility	7.38964e-012	7.38964e-012	0
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Iterations	5	5	7
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Extended solver state

Solver type	Branch and bound		
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Active	0	0	0
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Update interval	2	2	2
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GMU (K)	29	30	29
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ER (sec)	0	1	1
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Best objective	467.41	467.41	551.69
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Objective bound	467.41	467.41	551.69
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ESS	0	0	0
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TSI	5	5	7
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From Tables 82.4, 82.6 and 82.8 we can check that the best objective is achieved when ISP sets up either to fix the base price and quality premium to recover cost and to let user to choose the class; or to fix the base price and vary quality premium to

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recover cost and ISP can promote certain services by adding the condition to the models by setting up the sensitivity price for user  $j$  to be fixed and the sensitivity price for user  $i$  in class  $j$  to be varied.

## 82.4. Conclusion

From the above discussion, we can see that by considering the new parameters, decision variables and the constraints, we can obtain the better maximum profit. ISP can adopt either the model of modified by fixing  $\alpha$  and  $\beta$ ; or fixing  $\alpha$  and varying  $\beta$  for  $W_j$  as variable and fixing  $\alpha$  parameter to attain maximum value of 323.78 bps for each file and web traffic data.

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